

# Permutation of National Identification Number for a Better Security in Communication Channel

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**Abstract:-** This study proposes a new method to enhance the security of transmitting national identification number via various communication channels like SMS, email, and Box office. It introduces a permutation technique utilizing the Gamma 1 Non-Deranged Permutation group, ensuring the confidentiality of the information. By employing 11 factorial (11!) permutations, the national identification number is transformed into a mixed format for unintended recipients, yet remains easily decrypted by the intended recipient. This approach mitigates concerns regarding data interception and unauthorized access, providing a robust solution for secure information transmission across diverse media channels.

**Keywords:-** NIN, Permutation, Cryptography, Factorial, Non Deranged Permutation.

## I. INTRODUCTION

National Identity Management Commission (NIMC) as a national body in Nigeria is responsible for allocating the national identity number (NIN), an 11-digit number code (e.g.: 41134789082) designed and given to Nigerians and legal residents by government irrespective of their ages. The issuance of National identification Number, a National Identity or National Insurance Number by Nigerian government is in line with the global best practices in keeping a good track record of its citizen and those who resides both in permanent and temporary basis serving government in a variety of functions. The study of identification was extensively conducted by [8],[9],[10],[11].

The distribution and allocation of National Identification Number may vary among countries but the issuance of identification number is mostly done to citizens when they reach certain legal age or at the point of birth. Unlike non-citizens whom will be given identification upon entrance of a particular country or when a permanent or temporary resident permit is obtained. In some countries the purpose of issuing such numbers may be singular but in the long run the numbers may serve a National Identity. In United State of America, for example, the use of (SSN) i.e. Social Security Number system had been introduced in order to distribute and manage social security benefits. But over time a significant expansion of the widespread use of the SSN is recorded beyond its original purpose leading to the wide range of activities such as opening bank accounts, getting credit cards, driving permit to mention but a few. However,

in some countries the use of Tax Identification Number is necessary before any overseas payment procedure can be consummated; unlike in US where parameters like date of birth could serve without demanding for other nations' Tax Payer Identification Number. In countries where an established nationwide number failed to exist, the need to create their own number for each individual arise and the risk of mismatching people identity could be high.

In [6],[5],[4],[2] the study of cryptography was conducted, Cryptography was derived from two Greek words "Kryptos" which means "Hidden or Secret" and "Graphein" "to write" which is the art and science of making communication. Cryptography is a method or technique by which a message can be altered so that it becomes meaningless to anyone else but the intended recipient. This is done primarily in two basic ways, one is to change the position of letters or words in a message known as "Transposition" and the other is by substituting letters or words by different ones, known as "substitution" respectively. The science of encryption and decryption can be traced back all the way to year 2000BC in Egypt. In 2010, using the concept of Catalan numbers the scheme for prime numbers ( $p \geq 5$ ) was developed. They defined the generating function for  $G_p = \{w_i : i \in p - 1\}$  such that  $w_i = \left( (1)(1+i)_{mp} (1+2i)_{mp} \dots (1+(p-1)i)_{mp} \right)$  where  $m_p := \text{modulo}_p$ . Permutation of  $G_p$  was studied by [7],[12],[13],[14],[15]

In this research  $G_p$  permutation group was employed to secure NIN over the communication channel such as social media, emails, box office, etc. Cryptography is divided into two, Symmetric key cryptography and Asymmetric key cryptography. In Symmetric key cryptography single key is used between the sender and receiver, while the Asymmetric key cryptography each user is assigned a pair of keys, a public key and a private key, the public key is made known to all members, while the private key is hidden by the user (sender), the sender uses the public key to encrypt the message, while the receiver uses his own hidden (private) key to decrypt the message. In this work, we consider Symmetric key cryptographic approach.

## II. PRELIMINARIES

Let  $G_p = \{w_i : i \in p - 1\}$  be a structure such that each  $w_i$  is generated from the arbitrary set for any prime  $p \geq 5$ , using the scheme

$$w_i = ((1)(1+i)_{mp}(1+2i)_{mp} \dots (1+(p-1)i)_{mp})$$

Then each  $w_i$  is called a cycle and the elements in each  $w_i$  are distinct and called successors.

### ➤ Example

Using the above setting, if  $p = 11$ , then we have  $G_{11}$  as  $G_{11} = \{w_1, w_2, \dots, w_{10}\}$  where Since 0 and 5 in  $modulo_5$  are equivalent, thus instead of using 0 in  $modulo_p$  we will be using p.

- Cipher: - Is a method of transforming a message to conceal its meaning.
- Encryption: - Is the process of encoding an information.
- Decryption: - Is the process of converting a data into its original form.

- Plaintext: - Is an unencrypted information pending input into cryptographic algorithms.
- KEY: - A string of characters used within an encryption algorithm for altering data so that it appears random.
- TRANSPOSITION: The process of changing objects from one position to another.
- TRANSPOSITION CIPHER: - Is an encryption technique that rearranges the position of characters without altering the characters themselves.
- Example of transposition cipher is as follows.
- Plaintext: GOVERNMENT

Table 1: Plaintext

1	2	3	4	5	6	7	8	9	10
G	O	V	E	R	N	M	E	N	T

Table 2: Transposition

1	3	5	7	9	10	2	4	6	8
G	V	R	M	N	T	O	E	N	E

The resulting transposition will be "GVRMNTOEENE". The cipher process is given by the figure below:

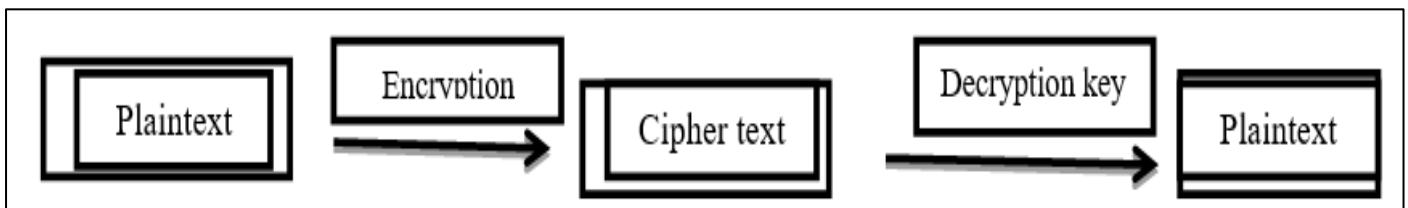


Fig 1: Cipher Algorithm

The above diagram represents Encryption and Decryption process of a Symmetric key cryptography.

### ➤ Experimental Result

- Let PT be a plaintext
- Let C be the ciphertext
- Let i be the key
- The Encryption Procedure to Take the Following Stages.
  - Applying encrypted function of  $G_p$  on PT will yield C, where the C is the ciphertext to be sent to the receiver.
  - The encrypted function obtained is given by

$$C: w_1 \rightarrow w_{1+i}, \quad i < p - 1$$

### ➤ The Decryption Procedure to Take the Following Stages.

- Reverse the encrypted function of  $G_p$  on C to obtain stacked ciphertext PT.
- The reversed function obtained is given by

$$PT: w_{1+i} \rightarrow w_1$$

By producing the PT the receiver can then use the national identification number used.

## III. ILLUSTRATION

Let:  
 PT: 35789426315

Where PT is a plaintext containing the NIN in which the encryption algorithm is to be applied.

### ➤ Encryption Stage

Applying encryption function of  $G_p$  on  $w_1$  ( $p = 11$ , number of characters and p is always a prime,)

$$G_{11} = \{w_1, w_2, w_3, \dots, w_{10}\}$$

Where

$$w_1 = (1\ 2\ 3\ 4\ 5\ 6\ 7\ 8\ 9\ 10\ 11)$$

$$w_2 = (1\ 3\ 5\ 7\ 9\ 11\ 2\ 4\ 6\ 8\ 10)$$

$$w_3 = (1\ 4\ 7\ 10\ 2\ 5\ 8\ 11\ 3\ 6\ 9)$$

$$w_4 = (1\ 5\ 9\ 2\ 6\ 10\ 3\ 7\ 11\ 4\ 8)$$

$$w_5 = (1\ 6\ 11\ 5\ 10\ 4\ 9\ 3\ 8\ 2\ 7)$$

$$w_6 = (1\ 7\ 2\ 8\ 3\ 9\ 4\ 10\ 5\ 11\ 6)$$

$$w_7 = (1\ 8\ 4\ 11\ 7\ 3\ 10\ 6\ 2\ 9\ 5)$$

$$w_8 = (1\ 9\ 6\ 3\ 11\ 8\ 5\ 2\ 10\ 7\ 4)$$

$$w_9 = (1\ 10\ 8\ 6\ 4\ 2\ 11\ 9\ 7\ 5\ 3)$$

$$w_{10} = (1\ 11\ 10\ 9\ 8\ 7\ 6\ 5\ 4\ 3\ 2)$$

$$C: w_1 \rightarrow w_{1+i}, \quad i < p - 1, \quad i = 4.$$

$$C: w_1 \rightarrow w_5$$

Where  $w_1$  is the PT

Table 3: The Table Below Shows the Permutation Values of  $w_1$

<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>
3	5	7	8	9	4	2	6	3	1	5

Table 4: The Table Below Shows the Permutation Values of  $w_5$

<b>1</b>	<b>6</b>	<b>11</b>	<b>5</b>	<b>10</b>	<b>4</b>	<b>9</b>	<b>3</b>	<b>8</b>	<b>2</b>	<b>7</b>
3	4	5	9	1	8	3	7	6	5	2

The ciphertext to be sent to the receiver is **34591837652<sub>4</sub>**, where the subscript <sub>4</sub> is to be used as a key for the decryption process.

➤ *Decryption Stage*

Reverse the encryption of **Gp** on the *C* to get *PT*

$$PT: w_{1+i} \rightarrow w_1$$

Table 5: The Table Below Shows the Permutation Values of  $w_5$

<b>1</b>	<b>6</b>	<b>11</b>	<b>5</b>	<b>10</b>	<b>4</b>	<b>9</b>	<b>3</b>	<b>8</b>	<b>2</b>	<b>7</b>
3	4	5	9	1	8	3	7	6	5	2

The table above is the table of permutation of NIN digits in which the sender is assumed to receive then use the decryption method and decode the coding process to use the original NIN numbers which was intended for concealing.

➤ *The Decryption Takes Place in Two Forms.*

- Identifying the key
- Using the key to decode the message  
 From (i) above, the message is **34591837652<sub>4</sub>** and the subscript is **4** which is the key used in the encoding process, and then we move to item (ii).
- $PT: w_{1+i} \rightarrow w_1$ , where  $(i = 4)$
- $PT: w_{1+4} \rightarrow w_1 : w_{4-1} \rightarrow w_1$
- And  $w_1$  is the final arrangement of the letters.

Table 6: Transposed NIN

<b>1</b>	<b>6</b>	<b>11</b>	<b>5</b>	<b>10</b>	<b>4</b>	<b>9</b>	<b>3</b>	<b>8</b>	<b>2</b>	<b>7</b>
3	4	5	9	1	8	3	7	6	5	2

Table 7: Decoded NIN

<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>
3	5	7	8	9	4	2	6	3	1	5

The above tables indicate the arrangements of the encoded and decoded NIN looks from the sender and receivers end.

**IV. RESULT AND DISCUSSION**

Encryption and decryption process goes through 2 processes, in the encryption stage, the original text(plaintext) will be encrypted with a special transposition cipher, then, there by producing a ciphertext which is more complex for cyber attackers but its easier for decryption by the intended recipient.

➤ *Mathematically the Process of Encryption and Decryption are as Follows*

- $C: w_1 \rightarrow w_{1+i}, i < p - 1,$  Encryption state of **Gp**.
- $PT: w_{1+i} \rightarrow w_1, i < p - 1,$  Decryption stage of **Gp**.

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