

Comprehensive Review of Medical Image Segmentation Topologies

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Abstract: Image segmentation is a crucial aspect of medical image analysis, primarily used to identify and evaluate affected tumors. It involves dividing an image into distinct regions that share similar features, allowing for the extraction of valuable information. A variety of image segmentation techniques have been developed, addressing the limitations of traditional medical segmentation methods. This paper reviews medical image segmentation techniques and the use of statistical mechanics through a novel approach known as the Lattice Boltzmann method (LBM). LBM is particularly advantageous due to its ability to significantly enhance computational speed in medical image segmentation while maintaining over 95% accuracy and specificity, outperforming conventional techniques. Given the limited research on LBM in medical physics, this paper aims to provide an overview of the progress made in this area.

Keywords: Segmentation, Computed Tomography, Magnetic Resonance Imaging, Image Processing, Image Analysis, Lattice Boltzmann Method.

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I. INTRODUCTION

Image processing techniques have gained increasing importance across a wide range of applications, driven by advanced methods and tools. Among these techniques, image segmentation stands out as a key area of focus. It involves dividing an image into distinct regions that are homogeneous in specific features, allowing for the extraction of valuable information. Image segmentation plays a crucial role in image analysis. In particular, medical imaging is vital to healthcare, contributing significantly to the field[1].

The quality of medical images plays a crucial role in diagnosis and treatment. Segmentation is an essential step in medical image analysis, designed to extract key details from images, enabling advanced understanding and interpretation. In scientific terms, segmentation is a mid-level vision task carried out by neurons, bridging low-level and high-level cortical processes, as shown schematically in Figure 1. For clinical images, segmentation aims to identify anatomical structures and delineate their boundaries in digital form. This is particularly vital in Radiotherapy (RT), where imaging is an integral part of the therapy process, helping identify the treatment target and surrounding healthy tissues to avoid unnecessary radiation exposure. Consequently, Radiotherapy Treatment Planning Systems (RTPS) require accurate anatomical data from CT scans to outline the treatment target and normal structures, with clinicians manually marking these areas[2]. Segmented images are then transferred to RTPS for radiation dose calculation, making precise segmentation essential for the success of patient treatment. In radiotherapy, segmentation quality directly affects spatial precision and the

accuracy of dose computations, both of which are tightly interrelated. The goal of image segmentation is to break down medical images into distinct components or objects with similar and consistent features. One of these features could be intensity or color, which helps identify anatomical structures, tumors, etc. The extent of segmentation depends on the specific application, and no single, universal theory for image segmentation exists. Numerous segmentation methods and algorithms have been proposed in the literature to overcome the limitations of traditional medical segmentation techniques. The choice of a specific method or algorithm depends on the type and nature of the image involved[3].

Recent developments in image segmentation techniques have been frequently reviewed, with a focus on categorizing methods based on the type of data they process (e.g., pixel or voxel data) and their applications in diagnosis, treatment planning, and follow-up. However, a notable challenge remains in the speed of computation. This paper provides a brief review of various medical image segmentation techniques, including thresholding, region-based methods, clustering, edge detection, model-based approaches, and the novel Lattice Boltzmann Method (LBM). The LBM, which is rooted in a microscopic understanding of macroscopic physical processes, aims to enhance computational efficiency. As there is no existing review on the progress of LBM in medical image segmentation, this paper presents an overview of this novel approach and encourages further exploration of LBM in medical image segmentation research[4].

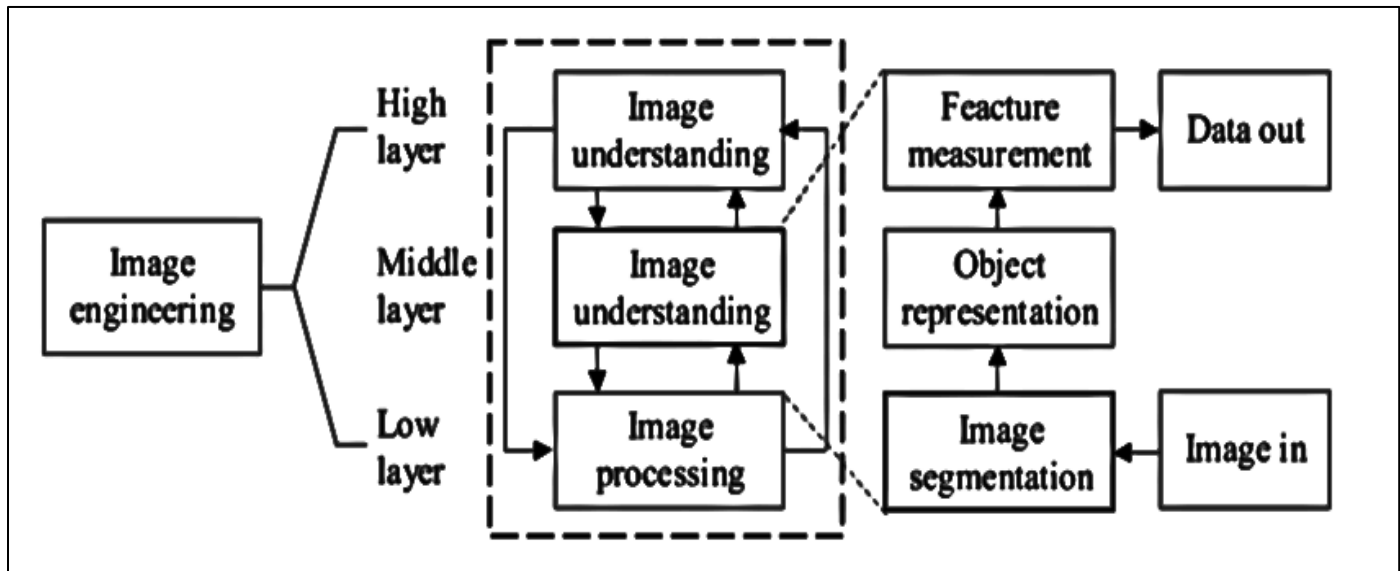


Fig 1 Image Engineering and Image Segmentation

II. SEGMENTATION TECHNIQUES

Recently, significant efforts have been focused on improving the image segmentation process. Various segmentation methods and algorithms have been discussed in the literature, each addressing the limitations of traditional medical segmentation techniques. However, there is no single "best" method suitable for all types of images; each technique is tailored to specific images and applications. Image segmentation techniques can be broadly categorized into Thresholding, Region Growing & Region Splitting and Merging, Clustering, Edge Detection, and Model-based methods. All segmentation techniques rely on two fundamental principles: intensity values and image characteristics such as discontinuity and similarity. The discontinuity-based approach segments an image by identifying sudden changes in intensity or grayscale levels, focusing primarily on detecting isolated points. In contrast, similarity-based techniques segment the image by grouping pixels that share similar values within a predefined range, with methods like Thresholding, Region Growing, and Region Splitting and Merging falling under this category[5].

III. THRESHOLDING

Thresholding is one of the fundamental methods used in image segmentation, where a single threshold value is applied to convert a grayscale image into a binary image. The key aspect of this process is selecting an appropriate threshold value (T). Pixels with intensities above this threshold are categorized as part of the foreground, while all other pixels are considered part of the background region. Several well-known techniques are commonly used in the industry, including "The Maximum Entropy Method", Otsu's method (which maximizes variance), and K-means clustering. While Thresholding segmentation performs effectively on images with sharp edges, it can be affected by noise and unclear boundaries. To mitigate the influence of noise, two common strategies are used: smoothing the image before applying Thresholding, and combining Thresholding with Edge Detection techniques.

IV. REGION-BASED METHODS

There are three key techniques for region-based image segmentation.

➤ Region Growing

In region growing algorithms, the segmentation process starts from a specific seed pixel, and the region's growth depends on the connectivity of neighboring pixels. This connectivity is based on similarity criteria, such as grayscale intensity, shape, size, or color, which are defined by thresholds to guide the expansion of the region. The choice of the seed point and the similarity criteria directly influences the segmentation results. By incorporating statistical information and prior knowledge, these algorithms can adapt based on the initial seed points, making the method more flexible and dynamic[6].

➤ Region Split and Merge Approach

The second region-based technique is the split and merge method. This approach uses a quadtree representation of the image, where the image is recursively divided into four quadrants. Each split takes into account the non-uniform characteristics of the image segment. When neighboring image regions are found to be uniform, they are merged into a single image composed of the four neighboring segments. The process continues until no further merging is possible. This method effectively reduces high-frequency artifacts, and the selection of seed points relies on local statistical information. It is commonly used for evaluating specific regions, such as breast tissue or cyst masses. These algorithms mainly depend on image intensity data to address partial volume effects and prevent leakage[7].

➤ Watershed Approach

Another region-based segmentation technique is the Watershed method, which treats the image as a topographic surface. In this approach, low-intensity pixels are interpreted as valleys, while high-intensity pixels are seen as hills or peaks. The algorithm begins by filling the valleys from local minima, with seeds acting as water sources. Each seed is assigned a unique color, and the water from these seeds floods

the surrounding regions. As the water from different seeds meets, a barrier is formed to prevent the merging of different regions, known as the watershed lines. This process continues until all peaks are submerged, and the barriers formed during the flooding process define the segmentation boundaries[8].

The Watershed algorithm combines information from both the gradient and grayscale levels of the image. The regions where water accumulates around local minima are called "catchment basins." The pixels in the grayscale image are treated as "water droplets," and the outcome of the catchment basins corresponds to segments of the image with similar pixel characteristics. There are two primary algorithmic processes used in the watershed method to handle the image[9]

➤ *Flooding in the Watershed Approach*

In the Watershed algorithm's rainfall process, local minima across the image are identified. Each local minimum is assigned a unique label, and neighboring pixels are linked to this label. A hypothetical water droplet is placed at each unmarked pixel, and it flows toward neighboring pixels with the lowest intensity, continuing until it reaches a marked pixel, at which point it adopts that marked value. During the flooding process, a single droplet is placed at each neighborhood minimum, and a flood of pixels expands outward from the pixel at the minimum. If the flood continues, excess pixels are discarded, and the process repeats. However, this method may not be effective for images with weak boundaries[10].

The standard Watershed method is susceptible to over-segmentation, particularly when images contain noise or when the objects within the image have a low signal-to-noise ratio. Over-segmentation can be minimized by applying appropriate filtering techniques, which remove irrelevant local minima. To overcome the challenges of traditional Watershed algorithms, enhanced versions, such as power watershed algorithms, have been developed, offering more precise segmentation results[11].

These advanced algorithms combine the benefits of unsupervised neural network (NN) classification with morphological Watershed segmentation, improving the accuracy of breast tumor contour detection in ultrasound images. A newer variant, the stochastic watershed approach, has been applied to enhance the accuracy of contour detection. By tuning optimal parameters through training, this method has demonstrated strong performance on 17 data sets, proving to be a robust tool for automatic liver segmentation, outperforming other approaches. Additionally, marker-controlled watershed algorithms, combined with distinctive feature combinations, have been successfully used for tumor extraction in brain MRI images.[12]

V. CLUSTERING APPROACH

Clustering refers to the process of grouping homogeneous data into clusters based on similarity criteria. One of the most commonly used clustering algorithms is "K-means clustering" (hard clustering), where each data point belongs exclusively to one cluster. In contrast, the soft clustering approach, such as the Fuzzy C-Means (FCM)

algorithm, allows a pixel to belong to more than one cluster. The degree to which a pixel belongs to a particular cluster is determined by a fuzzy membership function, with values ranging between 0 and 1. When a pixel's position is close to the centroid of a cluster, it can be assigned to that cluster if the membership function value approaches.[13]

The objective function in FCM is defined as the summation of the squared Euclidean distances between each sample and its corresponding cluster center, weighted by the fuzzy membership distances. The FCM algorithm is used to partition both grayscale and color images, with the number of clusters typically set in advance. If there is a deviation from the expected value, it can indicate potential shortcomings in the segmentation process.[14]

One of the strengths of FCM is its flexibility, as the objective function can be adjusted and extended to meet specific requirements. This variability makes FCM suitable for a wide range of image types. Additionally, the FCM algorithm includes mechanisms to assess the validity of the clustering results, making it a robust tool for segmentation tasks.[15]

The objective of clustering is to minimize computational effort while achieving satisfactory results. Refinements to the Fuzzy C-Means (FCM) algorithm have been made to improve its performance. Traditional FCM algorithms are sensitive to noise, especially in medical images like MR scans, where intensity heterogeneities may complicate segmentation. To address this, the Euclidean distance in FCM is replaced with a kernel-induced distance, resulting in the Kernelized Fuzzy C-Means (KFCM) algorithm. This modification enhances robustness by incorporating kernel methods to better handle variations in image intensity[16].

Additionally, a Fast Generalized Fuzzy C-Means (FGFCM) algorithm has been introduced, which integrates both local spatial and grayscale information. This approach effectively suppresses noise while preserving important image details, making it especially useful for medical imaging tasks. Various improvements have been tested, including the evaluation of these algorithms on CT brain images to identify abnormal regions and on bacterial images to separate bacteria from the background. The results showed that T2FCM (Type-II Fuzzy C-Means) efficiently removed noise, although it slightly increased the size of the segmented objects. IFCM (Intuitionistic Fuzzy C-Means) outperformed other methods in terms of segmentation accuracy.[17]

In another innovation, the Fuzzy-Based Artificial Bee Colony (FABC) algorithm was proposed, which combines Artificial Bee Colony (ABC) Optimization with Fuzzy C-Means (FCM). This approach uses the fuzzy membership function to optimize cluster centers through the ABC algorithm. When tested on synthetic and medical images, the results demonstrated that FABC outperforms other segmentation methods in terms of efficiency.[18]

Lastly, the ARKFCM (Adaptable Regularized Kernel Fuzzy C-Means) algorithm was introduced for brain MRI segmentation. This customizable, regularized kernel-based

method improves the algorithm's robustness, helping to preserve important image details and adapt to the complexity of medical images.[19]

VI. EDGE DETECTION

Edge detection is one of the most traditional methods used to identify irregularities or boundaries in an image. The boundary or transition between two regions with distinct intensity levels or grayscale values is known as an edge. Detecting these edges is crucial for various applications, including image enhancement, as it helps to highlight important details of an image. To detect edges, derivative operations are commonly used. Specifically, a convolution function is applied to the image using an appropriate mask.[20]

One of the most effective edge detectors is the Canny edge detector, which improves edge detection by using gradient magnitude thresholds to identify potential edges. It then refines these edges through non-maximal suppression and hysteresis thresholding. These processes help to suppress weak or irrelevant edge candidates, ensuring that only the most significant edges remain.[21]

However, noise in the image can have a significant impact on edge detection, often leading to fragmented or irregular edges that are not representative of the actual boundaries. To mitigate this, the image is typically smoothed using a Gaussian operator before edge detection is performed. This smoothing process helps to reduce noise, but it can also lead to false edge detections if not applied properly. To address this, multi-resolution edge detection and edge tracing techniques can be employed to improve the accuracy and consistency of the edge detection process.[22]

VII. MODEL-BASED ALGORITHMS

Model-based algorithms have emerged as some of the most effective strategies for image analysis, particularly when working with predefined models. These models are constructed based on prior knowledge and contain information about the expected features or structures in the image, such as the shape, texture, or behavior of the objects being analyzed. The core idea behind model-based approaches is to match or fit these models to the data in the image to extract meaningful information.[23]

By using a model, these algorithms can incorporate prior knowledge, making them more robust in situations where simple pixel-based methods might struggle. This is especially useful when dealing with complex images or in cases where there is limited contrast or noisy data. The model can be adapted or optimized based on the specific characteristics of the image, allowing for more accurate segmentation and detection of objects or anomalies.[24]

➤ *Markov Random Field Models*

Markov Random Field (MRF) models are a type of stochastic process where the distribution of future states depends solely on the current state, and not on how the system arrived at that state. An image sequence that follows this Markov property, where the current state dictates the

distribution of the next state, is referred to as a Markov Random Field (MRF). The MRF model is inspired by the Ising model and has been widely applied in image segmentation tasks due to its ability to preserve edges while approximating image parameters effectively.[24]

A key variant of MRF is the Hidden Markov Random Field (HMRF) model [31]. In HMRF, the states of the system are not directly observable, but can be inferred through analysis. Mathematically, the FM model can be considered a degraded version of the HMRF model. By integrating the HMRF model with the Expectation-Maximization (EM) algorithm into an HMRF-EM framework, researchers have achieved more precise and robust segmentation results. This approach has been compared to traditional FM model-based segmentation techniques, demonstrating improved accuracy.

Further advancements include the combination of MRF with Self-Organizing Feature Maps (SOFM), which incorporates spatial constraints to enhance the smoothness of image partitioning. Additionally, the use of Pickard Random Fields (PRF), an unsupervised variant of MRF, has been explored for mass breast segmentation. The PRF model has shown to be more efficient than traditional MRF in terms of computational complexity, providing a more practical solution for certain applications.[25]

In summary, MRF-based models, including their variants like HMRF and PRF, offer powerful tools for image segmentation, particularly in preserving structural details such as edges, while also benefiting from advanced algorithms that improve computational efficiency and accuracy.[26]

➤ *Artificial Neural Networks*

Artificial Neural Networks (ANNs) are mathematical models inspired by the structure and function of the human brain's neurons. Each node in an ANN function like a neuron and is connected to other nodes via communication links, with each link having a synaptic weight. The inputs to these synaptic weights are processed through an activation function to classify or identify objects within the image.

Two key features of ANNs are training and learning. In the training phase, the network is fed with attributes, often statistical in nature, such as mean, standard deviation, kurtosis, skewness, or transformed features obtained through Wavelet or Curvelet transforms. This phase, referred to as the "speculating phase," progresses until the network reaches a steady state, providing acceptable results based on the images being analyzed. During the learning phase, the weights between the interconnected neurons are adjusted to improve the network's performance by providing appropriate feedback. Learning in ANNs can be either supervised or unsupervised. [27]

However, one of the challenges in using neural networks is determining the appropriate architecture, including the network size, type, number of layers, and the overall structure. The selection of these components significantly influences the performance of the network in solving specific problems.

In medical imaging, ANNs have been applied in various tasks. For instance, the Group Method of Data Handling (GMDH) has been used to identify lungs in clinical images. Fuzzy neural networks have been shown to yield better segmentation results, especially in noisy environments. Additionally, the use of Support Vector Machine (SVM) classifiers in conjunction with ANN segmentation techniques has proven effective, with the added benefit of reduced processing time and memory usage.[28]

In the context of liver malignancy detection, a combination of the 3D fast marching algorithm and a single hidden layer feed-forward neural network was used for the segmentation of liver cancer from MR images. The results were validated against radiologist-delineated ground truth images and showed reduced time complexity and increased accuracy compared to other semi-automatic segmentation techniques.

Moreover, Deep Convolutional Neural Networks (DCNNs) have been successfully employed to detect glioblastomas in brain MR images, further demonstrating the power of neural networks in medical image segmentation and analysis.

➤ *Graph Cut Approach*

The fundamental concept of the graph cut algorithm involves applying tools from graph theory to partition an image into foreground and background regions. In graph theory, each pixel in the image is represented as a node, and the edges between these nodes represent the connections, with weights corresponding to the probability of a node being part of the foreground or background. These connections are made to a source (S) or sink (T), with the weights acting as the probability of the pixel being assigned to either segment. The algorithm promotes the similarity of pixels within the same segment, while encouraging dissimilar pixels to belong to different segments.[29]

Once the graph is constructed, the goal is to partition it by creating a minimal cut that divides the foreground from the background, requiring the least amount of effort. The segmentation process considers both hard constraints (such as known boundaries or region properties) and soft constraints (which relate to the region's general characteristics). When hard constraints are modified, the global optimization is recalculated based on the updated cost function, ensuring the segmentation remains accurate.

In the graph cut algorithm, the nodes represent the pixels, and the edges represent the weighted connections between them. By computing the global optimal minimum cut, the algorithm separates the object (foreground) from the background within the image. This technique has been successfully applied to fields such as photo and video editing as well as medical image processing.[30]

Several algorithms have been proposed to minimize the energy function within graph cuts. The first algorithm performs labeling among a set of arbitrary pixels, allowing for movement between these labeled pixels to minimize energy. The second algorithm requires smoothing to refine the segmentation. Various energy functions have been used

in this context, including truncated quadratic energy functions and models like the Potts model, which apply penalties to smoothness in the segmentation process. The results of these techniques are often compared against different annealing variants to assess their effectiveness.

One notable advantage of the graph cut algorithm is its ability to provide optimal segmentation when prior information about the foreground shape is available. For multi-region graph cut partitioning, a kernel mapping approach is used to transform image data. The objective function incorporates original data to evaluate the deviations of the modified image, with the optimization algorithm iterating between graph cut optimization and fixed-point iterations to update the region parameters. This approach has shown powerful performance compared to more complex modeling methods, while still benefiting from the computational efficiency of graph cuts.

This method has been validated and quantitatively compared using synthetic, natural, and medical images. Kernel mapping, in particular, has produced promising results in multi-region partitioning of brain MR images, showcasing the versatility and effectiveness of the graph cut approach in medical image segmentation.

➤ *Lattice Boltzmann Method (LBM)*

The Lattice Boltzmann Method (LBM) is a powerful simulation technique that offers high accuracy, widely applied in kinetic theory for simulating various systems [32]. It operates by providing a microscopic understanding of macroscopic physical processes. LBM seeks to bridge the gap between macroscopic and microscopic scales by considering the behavior of a group of particles rather than individual particles. This method models the movement of particles on a lattice grid, capturing both local interactions and the macroscopic behavior of fluids or other media. LBM has proven to be effective in simulating fluid dynamics, heat transfer, and other physical phenomena, making it an attractive approach for a range of applications, including medical image segmentation.[31]

➤ *Lattice Boltzmann Method (LBM) in Image Segmentation*

The Lattice Boltzmann Method (LBM) is a simulation technique that operates by considering the behavior of a collection of particles rather than tracking individual particles. In this method, the solution area is divided into lattices, and particle distributions reside at each lattice node. These particles move in specific directions, determined by the lattice alignment. The model is typically represented as $DnQm$, where "n" indicates the problem's dimension and "m" refers to the number of directions or linkages in the lattice.[32]

A core aspect of LBM is the equilibrium distribution function and the relaxation time (τ), which defines the type of problem being addressed. LBM provides an alternative to conventional mathematical methods for solving partial differential equations (PDEs). It offers faster computation, requires less memory, and is well-suited for parallel computation due to its particle-based approach. This makes LBM particularly efficient in applications such as image analysis.

➤ *In the context of image processing, LBM operates in two primary stages:*

- Streaming Stage: Particles or particle densities move from one node to another across the lattice.
- Collision Stage: Particles or densities are reorganized at each node.

These stages are governed by the LBM evolution equation, which involves the relaxation time (τ) and the source term (α), determining the particle movement. Notably, the state of each node at the next time step is influenced by its neighboring nodes.

➤ *LBM Applications in Image Processing*

In medical image segmentation, LBM can be particularly useful due to its ability to handle complex domains. Each pixel value in an image can be treated as a particle density, and changes in pixel values are seen as redistributions of these particles. LBM incorporates essential image features such as gradient and curvature information into the image segmentation process.

- Some applications of LBM in image processing include:

- ✓ Image Smoothing
- ✓ Image In painting
- ✓ Image Segmentation

Additionally, LBM models have been employed for anisotropic diffusion in image segmentation, demonstrating effectiveness in clinical images. A novel LBM approach using the D2Q19 lattice model has also been proposed for segmenting MRI and clinical images, closely resembling anisotropic diffusion, offering promising results in medical imaging segmentation tasks.[33]

LBM's ability to easily apply to complex and multiphase domains makes it an ideal candidate for various medical image segmentation challenges.

VIII. CONCLUSION

This paper provides an overview of various medical image segmentation techniques and introduces the novel Lattice Boltzmann Method (LBM) as a potential advancement for future exploration in the field of medical image segmentation. While the current methods are useful, none of the challenges in medical image segmentation have been completely solved, and all the algorithms discussed offer opportunities for further enhancement. The segmentation of medical images remains a complex issue, especially in real-time applications like diagnostics and radiotherapy, where accurate segmentation of different tissues around the tumor site and precise tumor boundary detection is crucial. As such, more innovative work is necessary to improve computational efficiency and speed.

The Lattice Boltzmann Method (LBM) stands out for its computational speed and model adaptability, ensuring high-quality image processing while using reasonable computational resources. LBM is uniquely suited for image processing due to its clear physical interpretation: pixel

values are treated as particle densities, and changes in pixel values correspond to particle redistribution. The process is influenced by relaxation time, which determines the nature of the problem being addressed. Additionally, the inclusion of a source term makes the LBM method directly applicable to a wide range of image segmentation tasks. This approach shows promising potential for further research and development, particularly in medical image analysis.

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