

Zero Acceptance Number Chained Quick Switching System Indexed By Six Sigma Quality Levels

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Abstract:-This article deals with Zero Acceptance Number chained quick switching system indexed by six sigma quality levels. A zero acceptance number ($Ac=0$), is well-known as a zero defect sampling plan ($d=0$), accept the units in the sample. It leads to the Chained Quick Switching System having zero acceptance numbers, assigned such as ChQSS-1 ($n_N, n_T; i$) system. The ChQSS-1 indexed by six sigma quality levels and relative slope (h_0) and Tables are constructing for easy selection method.

Keywords:-Chain Sampling; Producer's Risk; Consumer's Risk; Operating Characteristic Curve; Quick Switching System, Relative Slope, Six Sigma Levels.

I. INTRODUCTION

Acceptance Sampling Plans is instead of doing 100 percent inspection, taking a random sample from a lot based on the result of random whether accepts or reject the lot. Using this technique cost and time reduced.

A single sampling attributes plan needs an inspection of a random sample of size n items. In a $Ac=0$ plan, also called a defect less sampling plan. If the defective units in a sample 'd' are zero then accept a lot. The $Ac=0$ plan is the normal choice for safety-related inspection of products and services.

Hahn(1974)[5] provided that the $Ac=0$ plan needs the minimum sample size for a specified Limiting Quality (LQ) and consumer's risk (β) when compared to $Ac > 0$ single sampling plans, and other types of attribute sampling plans, for example, double and multiple sampling plans. In the most recent production processes are of high quality and the fraction defective is frequently well managed at low levels.

Dodge (1955)[1], Schilling (1978)[8] and Maciulla (2006)[6] have given their operating characteristic (OC) curves to the discriminatory power of $Ac=0$ plans is rather poor. Dodge's .

(1955)[1] also explained that chain sampling plan of type ChSP-1 improves the discriminatory power of the $Ac=0$ plan by permitting a rare defective unit as confirmed as the longer nonconformity spacing within sequences of lots.

II. A BRIEF EXPLANATION OF CHAINED QUICK SWITCHING SYSTEM

Govindaraju (1991) [2] has studied of a quick switching system using two zero acceptance number in single sampling plans. In this system, assigned as QSS-1 ($n_N, n_T; 0$), uses a zero acceptance number plan ($n_N, 0$) with sample size of n_N , for normal inspection and a larger sample size ($n_N, n_T; 0$), for tightened inspection. While a rejection below the normal ($n_N, 0$) plan move to the tighten ($n_T, 0$) plan for the next lot; or else, the normal inspection plan shall be prolonged.

Using the ChSP-1 plan, a defective unit is considered like a rare one when the previous $i(\geq 0)$ following samples are free from the defective units. The QSS-1 ($n_N, n_T; 0$), system does not utilize a lead to recognize an irregular defective unit. On the other hand, such a rule can be moreover deployed throughout the normal inspection period of a QSS-1 ($n_N, n_T; 0$), system. It directs to the Chained Quick Switching System having zero acceptance numbers, assigned such as ChQSS-1 ($n_N, n_T; i$) system. Six sigma, Senthil kumar and Esha Raffie (2012)[9] have studied six sigma quick switching variables sampling system ($n_\sigma, k_{T\sigma}, k_{N\sigma}$) the probability of acceptance of the lot is $1-3.4 \times 10^{-6}$, where (n, k_N) and (n, k_T), $k_T > k_N$ are respectively the normal and tightened single sampling plans. The method and procedure for designing the six sigma quick switching variables sampling system based on the given six sigma acceptable quality level and six sigma limiting quality level. Also Radhakrishnan and Sivakumaran (2010) [7] have studied a new procedure for the construction and selection of Link Sampling Plan (LSP) indexed through Six Sigma Quality Level-1 (SSQL-1) and Six Sigma Quality Level-2 (SSQL-2) are presented. Tables are constructed and presented for the easy selection of the plans.

A. Operating Procedure of the Chqss-1 ($n_N, n_T; i$) System Indexed By Six Sigma Quality Levels

Step1: Use Tightened plan with the sample n_T items and observe the number of defective items d_T .

Step 2: Count the defective items if $d_T=0$, then accept the current lot and move to the normal plan for the next lot.

Step 3: If the defective items $d_T > 0$ then reject the current lot and go on to the tightened plan for the next lot.

Step 4: In Normal Plan, Select the samples $d_T > 0$ items and examine the number of defective items d_N Check whether the defective items $d_N=0$ or not.

Step 5: If the defective items $d_N=0$ then accept the current lot and move to the normal plan for the next lot.

Step 6: If the defective items $d_N>1$ then reject the current lot and go on to the tightened plan for the next lot.

Step 7: If the defective items d_N or $d_T>0$ in any of their preceding samples. Reject the current lot and invoke the tightened plan for the next lot. If $d_N=d_T=0$ accept the current lot and continue the normal inspection plan for the next lot.

Where n_N - Normal plan sample size, d_N - Defective items in the normal sample, n_T - Tightened plan sample size, d_T - Defective items in the tightened sample.

B. Designing of ChQSS-1

For the procedures, mainly when there are lesser than i preceding lots, the above conditions are doubtful to be satisfied, and for this reason the ChSP-1 plan or the ChQSS-1 system also cannot be used. Since a consumer's approach, the make use of the tighter $(n_T,0)$ plan is needed for the initial periods until i or more preceding lots are accepted. Consumer's risk of accepting poor quality and it is higher than the actual consumer risk under the tightened plan and as well as the producer's risk also very high. To avoid these consequences, the steady state OC of the ChQSS-1 $(n_N, n_T; i)$ system will be equivalent to the QSS-1 system having $(n_T,0)$ plan for the tightened inspection level and the ChSP-1 (n_N, i) plan for the normal inspection level. Tightened inspection level plan $(n_T,0)$ OC function under Poisson probability as

$$P_T(p) = e^{-x_T} \tag{1}$$

Here, $x_T=n_Tp$. This estimation is applicable when $n_Tp \leq 5$, a situation well fitted in practice for the reason that the fraction defective is commonly low. Use the Poisson distribution is too accurate and exact when the OC function of the ChSP-1 (n_N, i) plan is for non conformities, equivalent OC function is

$$P_N(p) = e^{-x_N} + x_N e^{-x_N(i+1)} \tag{2}$$

Here, $x_N=n_Np$. Equation (2) is accurate for independent defective and is repeatedly a good estimate for defective units.

For a QSS-1 system, the possible number of lots under tightened inspection before a switch to normal inspection is given by

$$c_T(p) = \frac{1}{P_T(p)} \tag{3}$$

And the possible number of lots under normal inspection by a switch to tightened inspection is given by

$$c_N(p) = \frac{1}{(1 - P_N(p))} \tag{4}$$

With (3) & (4) equations, the stable state or combined OC function of the QSS-1 system is given by

$$P_a(p) = \frac{c_T(p)P_T(p) + c_N(p)P_N(p)}{c_T(p) + c_N(p)} = \frac{P_T(p)}{1 - P_N(p) + P_T(p)} \tag{5}$$

Using equations (1) & (2) values into (5), notice that the stable state OC function of the ChQSS-1 $(n_N, n_T; 0)$ system

$$\text{turn into } P_a(p) = \frac{e^{-x_T}}{1 - e^{-rx_T} - rx_T e^{-rx_T(i+1)} + e^{-x_T}} = 1 - \square = 0.9999966 \tag{6}$$

$$P_a(p) = \frac{e^{-x_T}}{1 - e^{-rx_T} - rx_T e^{-rx_T(i+1)} + e^{-x_T}} = \beta = 0.0000068 \tag{7}$$

Here, $r = \frac{n_N}{n_T}$ is the ratio of normal inspection sample size to the tightened inspection sample size.

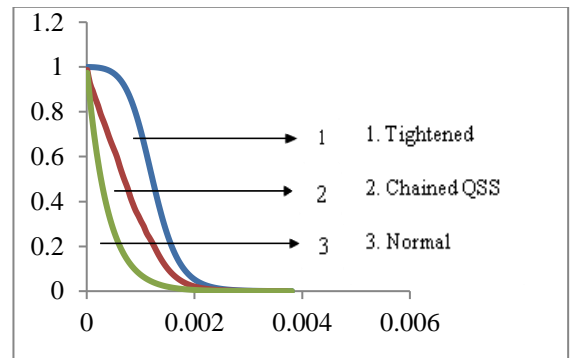


Fig-1: OC Curve of the Chqss-1(523, 2613; 5) System

From the above Fig-1 indicates the OC curve of the ChQSS-1(523,2613;5) system together with the (2613,0) single sampling plan for the tightened inspection level, and the ChSP-1 (523,5) plan for the normal inspection level. It is obvious to the stable state OC curve of the ChQSS-1(523,2613;5) system is nearer to the OC curve of the ChSP-1 (523,5) plan at high-quality levels except moves in the direction of the OC curve of the tightened inspection plan (2613,0) while the incoming quality go down. Next to good quality levels, the ChQSS-1 system uses a smaller sample size n_N and therefore performs more similar to a ChSP -1 plan permitting simply rare defective units. On poor quality levels, the ChQSS-1 system uses a larger sample size n_T and for this reason performs further similar to a zero acceptance number plan rejecting any defective item can say this, the ChQSS-1 system combine the useful characteristic of the ChSP-1 and $Ac=0$ plans at good in addition to poor quality levels. On the other hand, the ChQSS-1 system is not especially useful at reasonable quality levels (at which the probability of acceptance is neither too high nor low) since the OC curve of the ChQSS-1 system basically lies in the middle of the normal and tightened plans.

C. Evaluation of the Chained Quick Switching System

Let p_1 be the acceptance quality limit (AQL) and α be the producer’s risk of rejecting lots of p_1 quality. In addition, allow p_2 be the limiting quality and β is the consumer’s risk of accepting lots of p_2 quality. In this the operating ratio $\frac{P_2}{P_1}$ corresponding to the required producer risk and consumer risk is an opposite measure in a good way a sampling system differentiate among good and poor quality

lots. For an established ChQSS-1($n_T, n_T; i$) system, the operating ratio p_2/p_1 can be calculated using (6) & (7) in the below steps:

1. For the needed α , and for specified r and i solve $P_a(p_1)=0.9999966$ for $x_T=x_{1T}=n_T p_1$.
2. For the required β , and for specified r and i solve $P_a(p_2) = 0.0000068$ for $x_T=x_{2T}=n_T p_2$.
3. Find the operating ratio $\frac{P_2}{P_1} = \frac{x_{2T} x_{1T}}{p_1}$.

i	r=0.1	r=0.2	r=0.3	r=0.4	r=0.5	r=0.6	r=0.7	r=0.8	r=0.9	r=1
0	0.0261	0.0131	0.0085	0.0064	0.0052	0.0043	0.0037	0.0032	0.0029	0.0026
1	0.0151	0.0075	0.005	0.0038	0.003	0.0025	0.0021	0.0019	0.0017	0.0015
2	0.0116	0.0058	0.0039	0.0029	0.0023	0.0019	0.0016	0.0015	0.0013	0.0012
3	0.0099	0.0049	0.0033	0.0025	0.002	0.0016	0.0014	0.0012	0.0011	0.001
4	0.0086	0.0043	0.0029	0.0022	0.0017	0.0014	0.0012	0.0011	0.001	0.0009
5	0.0079	0.0039	0.0026	0.002	0.0016	0.0013	0.0011	0.001	0.0009	0.0008
6	0.0073	0.0036	0.0024	0.0018	0.0014	0.0012	0.001	0.0009	0.0008	0.0007
7	0.0068	0.0034	0.0022	0.0017	0.0013	0.0011	0.001	0.0008	0.0007	0.0007
8	0.0064	0.0031	0.0021	0.0016	0.0013	0.0011	0.0009	0.0008	0.0007	0.0006
9	0.006	0.003	0.002	0.0015	0.0012	0.001	0.0009	0.0007	0.0007	0.0006
∞	0.0041	0.002	0.0014	0.001	0.0008	0.0007	0.0006	0.0005	0.0005	0.0004

Table 1: Indexed By Six Sigma Quality Levels Values of $n_T p_1$ For Given (i, r)

i	r=0.1	r=0.2	r=0.3	r=0.4	r=0.5	r=0.6	r=0.7	r=0.8	r=0.9	r=1
0	12.882	12.248	12.011	11.935	11.9	11.899	11.891	11.889	11.88	11.868
1	12.398	11.999	11.923	11.902	11.888	11.886	11.885	11.884	11.862	11.862
2	12.283	11.985	11.907	11.898	11.875	11.874	11.872	11.872	11.858	11.853
3	12.253	11.98	11.9	11.895	11.869	11.868	11.866	11.865	11.847	11.844
4	12.249	11.975	11.881	11.88	11.852	11.851	11.851	11.841	11.836	11.829
5	12.247	11.966	11.793	11.791	11.783	11.78	11.779	11.778	11.777	11.775
6	12.238	11.952	11.79	11.788	11.78	11.777	11.769	11.766	11.764	11.762
7	12.226	11.898	11.778	11.777	11.763	11.761	11.755	11.754	11.752	11.752
8	12.193	11.878	11.69	11.688	11.675	11.674	11.671	11.671	11.668	11.662
9	12.187	11.86	11.686	11.677	11.668	11.664	11.663	11.661	11.654	11.652
∞	12.176	11.852	11.673	11.669	11.655	11.653	11.652	11.65	11.641	11.641

Table 2: Indexed By Six Sigma Quality Levels Values of $N_T p_2$ for Given (I, R)

In equation (6) explains the values of $n_T p_1$ for $\alpha = 0.9999966$ and for different (i, r) . Equation (7) reveals that the values of $n_T p_2$ for different combinations of (i, r) . The operating ratios attainable by a QSS-1 $(n_T, n_T; i)$ system are put into a Table 3. Operating ratios in the range 3-13 are not attainable by a QSS-1 $(n_N, n_T; 0)$ system. Where, Table 3 explains that the method of chaining lot results can attain for instance small operating ratios.

i	r=0.1	r=0.2	r=0.3	r=0.4	r=0.5	r=0.6	r=0.7	r=0.8	r=0.9	r=1
0	4.93	9.38	14.07	18.58	22.94	27.65	31.99	36.85	40.95	45.84
1	8.227	15.99	23.8	31.27	39.55	48.01	55.59	63.59	71.07	79.03
2	10.59	20.61	30.35	40.36	51.39	61.74	72.3	81.76	92.42	102
3	12.37	24.34	35.99	48.21	60.84	72.63	84.4	96.54	107.6	120.5
4	14.2	27.79	41.3	54.05	68.35	82.36	98.02	110	123.1	137.3
5	15.46	30.81	45.48	60.19	75.58	89.86	104.8	119.8	134.8	150.8
6	16.75	33.18	49.31	64.59	81.58	97.66	114	130.2	147.6	162.7
7	17.95	34.98	53.06	69.15	87.65	105.4	122.2	139.9	157.2	174.4
8	19.09	38.07	55.16	73	92.73	110.8	130.7	147.5	166.1	184.4
9	20.26	40.12	58.81	77.21	98.63	118.1	136.7	157.8	175.4	195.9
∞	29.93	58.59	85.96	115.9	143.2	171.7	199.9	229.2	257.3	283.2

Table 3: Indexed By Six Sigma Quality Levels Operating Ratios $\frac{P_2}{P_1} \%$ For Given (I, R)

i	r = 0.1	r=0.2	r=0.3	r =0.4	r=0.5	r=0.6	r=0.7	r=0.8	r=0.9	r=1
0	9.068	8.304	7.97	7.801	7.699	7.657	7.63	7.615	7.607	7.603
1	8.476	7.917	7.728	7.655	7.624	7.609	7.605	7.602	7.601	7.6
2	8.302	7.851	7.705	7.648	7.622	7.608	7.604	7.6	7.6	7.599
3	8.234	7.838	7.703	7.647	7.622	7.605	7.603	7.6	7.599	7.598
4	8.204	7.835	7.702	7.646	7.621	7.604	7.602	7.598	7.598	7.597
5	8.192	7.834	7.7	7.645	7.619	7.603	7.601	7.597	7.596	7.595
6	8.186	7.833	7.699	7.644	7.618	7.602	7.601	7.596	7.595	7.594
7	8.182	7.832	7.698	7.643	7.617	7.602	7.6	7.589	7.584	7.583
8	8.181	7.831	7.696	7.64	7.616	7.601	7.6	7.588	7.583	7.582
9	8.181	7.83	7.694	7.64	7.615	7.6	7.599	7.587	7.582	7.582
∞	8.18	7.83	7.693	7.638	7.614	7.599	7.598	7.586	7.582	7.581

Table 4: Indexed By Six Sigma Quality Levels Values of X_0 For Given N(I, R)

In 1950, Hamaker [4] presented an alternative method for calculating the power of difference between good and bad lots realized by a sampling plan. Let p_0 be the indifference quality level (IQL), the quality level at which the probability of acceptance and rejection are both equal to 50%. The “relative” slope of the OC curve at p_0 is described as

$$h_0 = -\left(\frac{p}{P_a(p)} \frac{dP_a(p)}{dp}\right)_{p=p_0} = -\left(2np \frac{dP_a(p)}{d(np)}\right)_{p=p_0}$$

$$= -\left(2np \frac{e^{-x_0}}{1 - e^{-rx_0} - rx_0 e^{-rx_0(i+1)} + e^{-x_0}} dx_0\right) - 2$$

$$\frac{\frac{x_0(i+1)r^2}{e^{rx_0(i+1)}} - \frac{r}{e^{rx_0(i+1)}} + \frac{r}{e^{rx_0}} - \frac{1}{e^{x_0}}}{e^{x_0} \left(\frac{rx_0}{e^{rx_0(i+1)}} - \frac{1}{e^{rx_0}} + \frac{1}{e^{x_0}} + 1\right)^2} - \frac{1}{e^{x_0} \left(\frac{rx_0}{e^{rx_0(i+1)}} - \frac{1}{e^{rx_0}} + \frac{1}{e^{x_0}} + 1\right)} \dots\dots\dots (9)$$

The relative slope h_0 is a direct measure of difference attained by a sampling plan. Used for the ChQSS-1 $(m_T, n_T; i)$ system, the “unity” value $x_T = n_T p_0 (= x_0 \text{ say})$ equivalent to the IQL can be obtained by equations (6) to 0.5 and solving for x_0 . The relative slope h_0 can be calculated using (6) and (7). From the Tables 4 and 5 explain x_0 and h_0 values, correspondingly, for the (i, r) arrangements revealed in

Table 1-3. From Table-5 verifies that the h_0 values for the ChQSS-1 $(m_T, n_T; i)$ systems are larger than the h_0 of the

QSS-1 $(n_N, n_T; 0)$ systems. This denotes that the method of chaining normal inspection sample outcomes directs to developed difference good and bad lots.

i	r=0.1	r=0.2	r=0.3	r=0.4	r=0.5	r=0.6	r=0.7	r=0.8	r=0.9	r=1
0	0.0105	0.0094	0.0087	0.0083	0.0081	0.0079	0.0078	0.0077	0.0077	0.0076
1	0.0096	0.0086	0.0081	0.0078	0.0077	0.0077	0.0076	0.0076	0.0076	0.0076
2	0.0092	0.0083	0.008	0.0078	0.0077	0.0077	0.0076	0.0076	0.0076	0.0076
3	0.009	0.0083	0.008	0.0078	0.0077	0.0077	0.0076	0.0076	0.0076	0.0076
4	0.0089	0.0083	0.008	0.0078	0.0077	0.0077	0.0076	0.0076	0.0076	0.0076
5	0.0089	0.0082	0.008	0.0078	0.0077	0.0077	0.0077	0.0076	0.0076	0.0076
6	0.0089	0.0082	0.008	0.0078	0.0077	0.0077	0.0077	0.0077	0.0076	0.0076
7	0.0089	0.0083	0.008	0.0078	0.0077	0.0077	0.0077	0.0077	0.0077	0.0077
8	0.0088	0.0083	0.008	0.0078	0.0077	0.0077	0.0077	0.0077	0.0077	0.0077
9	0.0088	0.0083	0.008	0.0079	0.0078	0.0077	0.0077	0.0077	0.0077	0.0077
∞	0.0088	0.0083	0.008	0.0079	0.0078	0.0077	0.0077	0.0077	0.0077	0.0077

Table -5: Indexed By Six Sigma Quality Levels Values of h_0 For Given $n(i, r)$

III. CONCLUSION

This reveals that the discriminatory power of a quick switching system including the zero acceptance number reference plan is developed when preceding lot results are chained chqss-1 systems are considered to control the producer’s and consumer’s risks or to minimise the sampling inspection effort.

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