

# A Novel Adaptive Sine Cosine Algorithm for Global Numerical Optimization

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**Abstract:-**A novel population based optimization algorithm known as Sine Cosine Algorithm (SCA), in contrast to meta-heuristics; main feature is randomization having a relevant role in both exploration and exploitation in optimization problem. A novel randomization technique termed adaptive technique is integrated with SCA and exercised on unconstrained test benchmark function and localization of partial discharge in transformer like geometry. SCA algorithm has quality feature that it uses simple trigonometric terms like sine and cosine term for every unconstrained and complex constrained optimization problem. Integration of new randomization adaptive technique provides potential that ASCA algorithm to attain global optimal solution and faster convergence with less parameter dependency. Adaptive SCA (ASCA) solutions are evaluated and results shows its competitively better performance over standard SCA optimization algorithms.

**Keywords:-**Meta-heuristic; Sine Cosine Algorithm; Adaptive technique; Global optimal; Benchmark function; Transformer.

## I. INTRODUCTION

A novel population based Sine Cosine algorithm [1] based on simple sine and cosine terms for both exploration and exploitation in optimization problem. In this algorithm random value plays very important role and integrated with adaptive technique that it changes position of current solution towards destination solution according to its fitness function.

In the meta-heuristic algorithms, randomization play a very important role in both exploration and exploitation where more strengthen randomization techniques are Markov chains, Levy flights and Gaussian or normal distribution and new technique is adaptive technique. So meta-heuristic algorithms on integrated with adaptive technique results in less computational time to reach optimum solution, local minima avoidance and faster convergence.

In past, many optimization algorithms based on gradient search for solving linear and non-linear equation but in gradient search method value of objective function and

constraint unstable and multiple peaks if problem having more than one local optimum.

Population based SCA is a meta-heuristic optimization algorithm has an ability to avoid local optima and get global optimal solution that make it appropriate for practical applications without structural modifications in algorithm for solving different constrained or unconstrained optimization problems. SCA integrated with adaptive technique reduces the computational times for highly complex problems.

Paper under literature review are: Adaptive Cuckoo Search Algorithm (ACSA) [2] [3], QGA [4], Acoustic Partial discharge (PD) [5] [6], HGAPSO [7], PSACO [8], HSABA [9], PBILKH [10], KH-QPSO [11], IFA-HS [12], HS/FA [13], CKH [14], HS/BA [15], HPSACO [16], CSKH [17], HS-CSS [18], PSOHS [19], DEKH [20], HS/CS [21], HSBBO [22], CSS-PSO [23] etc.

Recently trend of optimization is to improve performance of meta-heuristic algorithms [24] by integrating with chaos theory, Levy flights strategy, Adaptive randomization technique, Evolutionary boundary handling scheme, and genetic operators like as crossover and mutation. Popular genetic operators used in KH [25] that can accelerate its global convergence speed. Evolutionary constraint handling scheme is used in Interior Search Algorithm (ISA) [26] that avoid upper and lower limits of variables.

The remainder of this paper is organized as follows: The next Section describes the Sine Cosine algorithm and its algebraic equations are given in Section 2. Section 3 includes description of Adaptive technique. Section 4 consists of simulation results of unconstrained benchmark test function, convergence curve and tables of results compared with source algorithm. In Section 5 PD localization by acoustic emission, in section 6 conclusion is drawn. Finally, acknowledgment gives regards detail and at the end, references are written.

**II. SINE COSINE ALGORITHM (SCA)**

Newly proposed algorithm by SeyedaliMirjalili known as Sine Cosine Algorithm (SCA) simply based on Sine Cosine function used for exploration and exploitation phases in optimization problems.

$$X_i^{t+1} = X_i^t + r_1 \times \sin(r_2) \times |r_3 P_i^t - x_i^t| \quad (1)$$

$$X_i^{t+1} = X_i^t + r_1 \times \cos(r_2) \times |r_3 P_i^t - x_i^t| \quad (2)$$

Where:

$X_i^t$ : Location of current solution at  $t$ -th iteration in  $i$ -th dimension,  $r_1, r_2, r_3$  random value,  $P_i$  location of targeted optimal solution. Equation (1) and Equation (2) uses  $r_1 \leq 0.5$ ,  $r_1 \geq 0.5$  condition for exploration and exploitation.

**III. ADAPTIVE SCA ALGORITHM**

In the meta-heuristic algorithms, randomization play a very important role in both exploration and exploitation where more randomization techniques are Markov chains, Levy flights and Gaussian or normal distribution and new technique is adaptive technique. Adaptive technique used by Pauline Ong in Cuckoo Search Algorithm (CSA) [2] and shows improvement in results of CSA algorithms. The Adaptive technique [3] includes best features like it consists of less parameter dependency, not required to define initial parameter and step size or position towards optimum solution is adaptively changes according to its functional fitness value over the course of iteration. So meta-heuristic algorithms on integrated with adaptive technique results in less computational time to reach optimum solution, local minima avoidance and faster convergence.

$$X_i^{t+1} = X_i^t + randn * \left(\frac{1}{t}\right)^{((bestf(t) - fi(t))/(bestf(t) - worstf(t)))} \quad (3)$$

Where

$X_i^{t+1}$  new solution of  $i$ -th dimension in  $t$ -th iteration  $f(t)$  is the fitness value

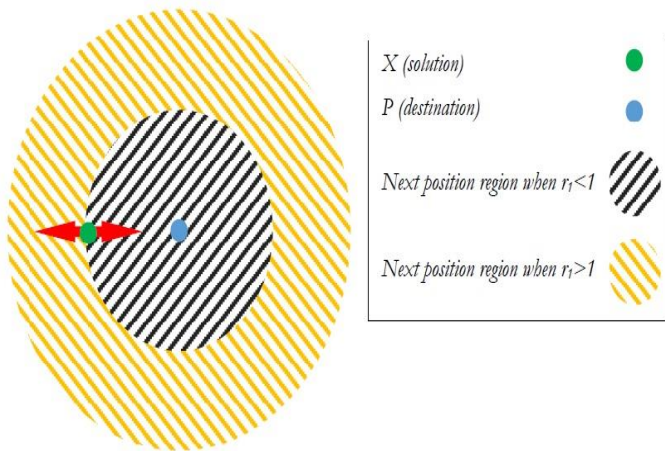


Fig.1: Illustrating Next Step Towards Targeted Optimum Solution

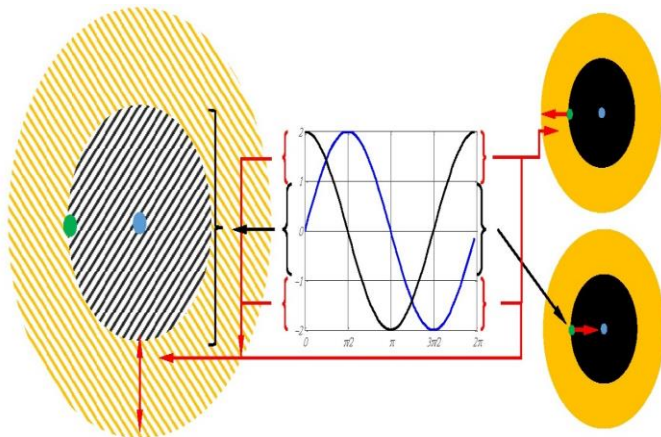


Fig.2: Basic Principle of SCA Algorithm

**IV. SIMULATION RESULTS FOR UNCONSTRAINT TEST BENCHMARK FUNCTION**

No.	Name	Function	Dim	Range	Fmin
F1	Sphere	$f(x) = \sum_{i=1}^n x_i^2 * R(x)$	10	[-100, 100]	0
F2	Schwefel 2.22	$f(x) = \sum_{i=1}^n  x_i  + \prod_{i=1}^n  x_i  * R(x)$	10	[-10, 10]	0
F3	Schwefel 1.2	$f(x) = \sum_{i=1}^n \left( \sum_{j=1}^i x_j \right)^2 * R(x)$	10	[-100, 100]	0
F4	Schwefel 2.21	$f(x) = \max_i \{ x_i , 1 \leq i \leq n\}$	10	[-100, 100]	0
F5	Rosenbrock's Function	$f(x) = \sum_{i=1}^{n-1} \left[ 100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2 \right] * R(x)$	10	[-30, 30]	0
F6	Step Function	$f(x) = \sum_{i=1}^n ([x_i + 0.5])^2 * R(x)$	10	[-100, 100]	0
F7	Quartic Function	$f(x) = \sum_{i=1}^n ix_i^4 + random[0,1] * R(x)$	10	[-1.28, 1.28]	0
F8	Schwefel 2.26	$F(x) = \sum_{i=1}^n -x_i \sin(\sqrt{ x_i }) * R(x)$	10	[-500, 500]	(-418.9829 *5)
F9	Rastrigin	$F(x) = \sum_{i=1}^n [x_i^2 - 10 \cos(2\pi x_i) + 10] * R(x)$	10	[-5.12, 5.12]	0
F10	Ackley's Function	$F(x) = -20 \exp \left( -0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2} \right) - \exp \left( \frac{1}{n} \sum_{i=1}^n \cos(2\pi x_i) \right) + 20 + e * R(x)$	10	[-32, 32]	0
F11	Griewank Function	$F(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos \left( \frac{x_i}{\sqrt{i}} \right) + 1 * R(x)$	10	[-600, 600]	0

<b>F12</b>	Penalty 1	$F(x) = \frac{\pi}{n} \left\{ \begin{array}{l} 10\sin(\pi y_1) + \sum_{i=1}^{n-1} (y_i - 1)^2 \\ [1 + 10\sin^2(\pi y_{i+1})] + (y_n - 1)^2 \end{array} \right\}$ $y_i = 1 + \frac{x_i + 1}{4},$ $u(x_i, a, k, m) = \begin{cases} k(x_i - a)^m & x_i > a \\ 0 & -a < x_i < a \\ k(-x_i - a)^m & x_i < -a \end{cases}$	10	[-50, 50]	0
<b>F13</b>	Penalty 2	$F(x) = 0.1 \left\{ \begin{array}{l} \sin^2(3\pi x_1) + \sum_{i=1}^n (x_i - 1)^2 \\ [1 + \sin^2(3\pi x_i + 1)] \\ + (x_n - 1)^2 [1 + \sin^2(2\pi x_n)] \end{array} \right\}$ $+ \sum_{i=1}^n u(x_i, 5, 100, 4) * R(x)$	10	[-50, 50]	0
<b>F14</b>	De Jong (Shekel's Foxholes)	$F(x) = \left( \frac{1}{500} + \sum_{j=1}^{25} \frac{1}{j + \sum_{i=1}^2 (x_i - a_{ij})^6} \right)^{-1}$	2	[-65.536, 65.536]	1
<b>F15</b>	Kowalik's Function	$f(x) = \sum_{i=1}^{11} a_i - \left[ \frac{x_i (b_i^2 + b_i x_2)}{b_i^2 + b_i x_3 + x_4} \right]^2$	4	[-5,5]	0.00030
<b>F16</b>	Branin Function	$f(x) = \left( x_2 - \frac{5.1}{4\pi^2} x_1^2 + \frac{5}{\pi} x_1 - 6 \right)^2 + 10 \left( 1 - \frac{1}{8\pi} \right) \cos x_1 + 10$	2	[-5,0] [10,15]	0.398
<b>F17</b>	Goldstein and Price Function	$f(x) = \left[ \begin{array}{l} 1 + (x_1 + x_2 + 1)^2 \\ (19 - 14x_1 + 3x_1^2 - \\ 14x_2 + 6x_1x_2 + 3x_2^2) \end{array} \right]^*$ $\left[ \begin{array}{l} 30 + (2x_1 - 3x_2)^2 \\ * (18 - 32x_1 + 12x_1^2 + \\ 48x_2 - 36x_1x_2 + 27x_2^2) \end{array} \right]$	2	[-2,2]	3

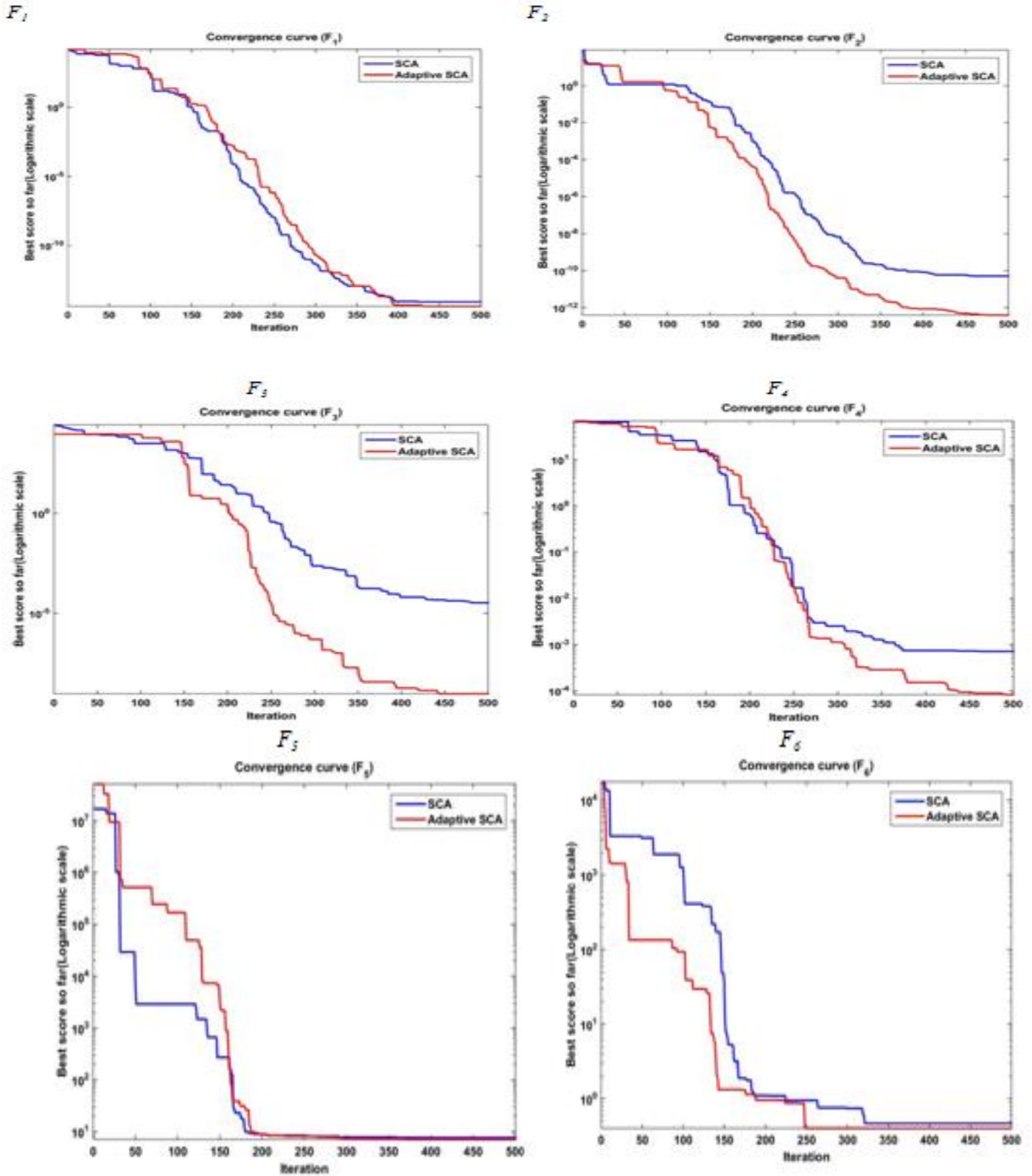
<b>F18</b>	Hartman 1	$f(x) = -\sum_{i=1}^4 c_i \exp\left(-\sum_{j=1}^3 a_{ij} (x_j - p_{ij})^2\right)$	3	[0,1]	-3.86
<b>F19</b>	Hartman 2	$f_{20}(x) = -\sum_{i=1}^4 c_i \exp\left(-\sum_{j=1}^6 a_{ij} (x_j - p_{ij})^2\right)$	6	[0,1]	-3.32
<b>F20</b>	Shekel 1	$f(x) = -\sum_{i=1}^5 \left[ (X - a_i)(X - a_i)^T + c_i \right]^{-1}$	4	[0,10]	-10.1532
<b>F21</b>	Shekel	$f(x) = -\sum_{i=1}^7 \left[ (X - a_i)(X - a_i)^T + c_i \right]^{-1}$	4	[0,10]	-10.4028
<b>F22</b>	Shekel	$f(x) = -\sum_{i=1}^{10} \left[ (X - a_i)(X - a_i)^T + c_i \right]^{-1}$	4	[0,10]	-10.5363
<b>F23</b>	Cube function	$f(x) = 100(x_2 - x_1^3)^2 + (1 - x_1)^2$	30	[-100, 100]	0
<b>F24</b>	Matyas function	$f(x) = 0.26(x_1^2 + x_2^2) - 0.48x_1x_2$	30	[-30, 30]	0
<b>F25</b>	Powell function	$f(x) = \sum_{i=1}^{D-2} \left\{ (x_{i-1} + 10x_i)^2 + 5(x_{i+1} - x_{i+2})^2 + (x_i - 2x_{i+1})^4 + 10(x_{i-1} - x_{i+2})^4 \right\}$	4	[-30, 30]	0
<b>F26</b>	Beale Function	$f(x) = \left\{ \begin{aligned} &(1.5 - x_1 + x_1x_2)^2 + (2.25 - x_1 + x_1x_2^2)^2 \\ &+ (2.625 - x_1 + x_1x_2^3)^2 \end{aligned} \right\}$	30	[-100, 100]	0
<b>F27</b>	levy13 function	$f(x) = \left\{ \begin{aligned} &\sin^2(3\pi x_1) + (x_1 - 1)^2 (1 + \sin^2(3\pi x_2)) \\ &+ (x_2 - 1)^2 (1 + \sin^2(2\pi x_2)) \end{aligned} \right\}$	30	[-10, 10]	0

Table 1: Benchmark Test Functions

Parameter Name	Search Agents no.	Max. Iteration no.	No. of Evolution
F1-F27	30	500	20-30
Acoustic PD Localization	40	200	30

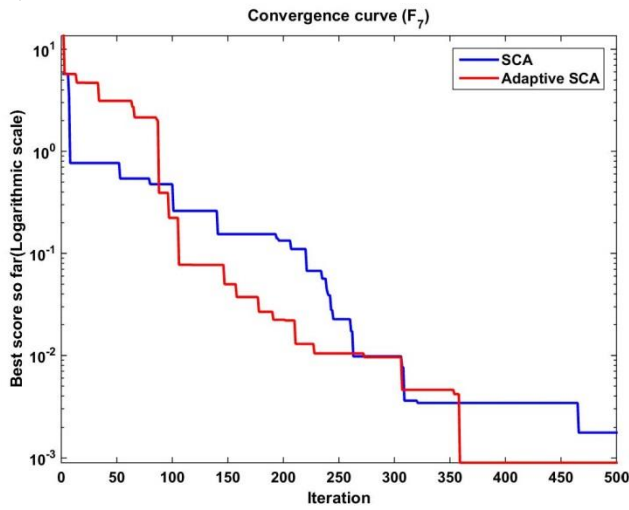
**Note:-** Scale specified on axis, Not specified means axis are linear scale

Table 2: Internal Parameters

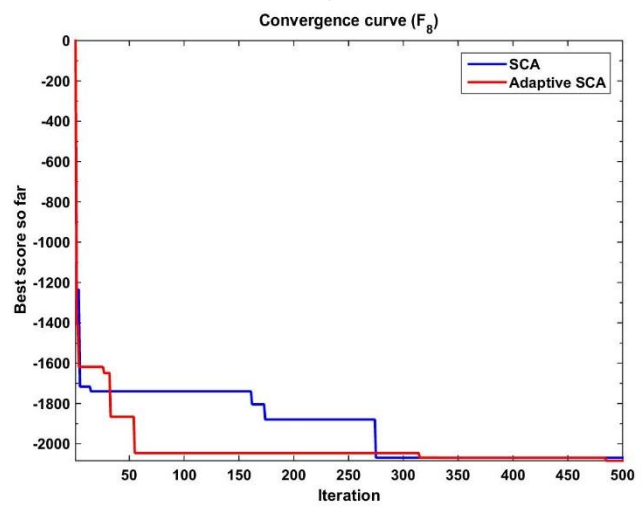




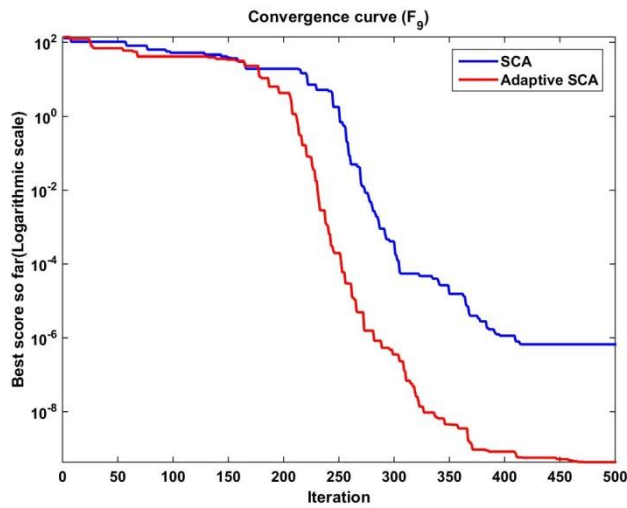
$F_7$



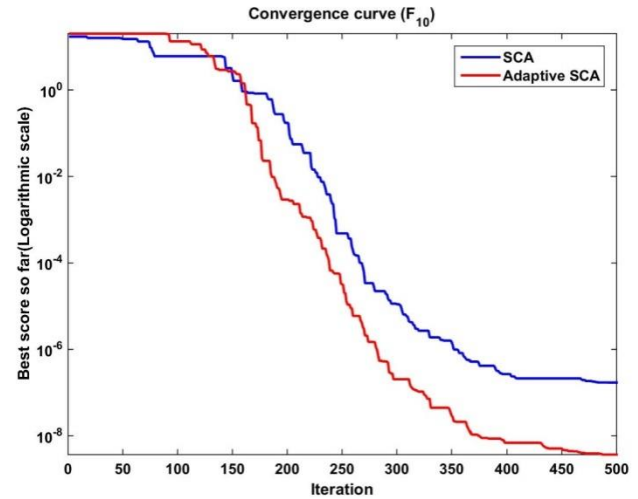
$F_8$



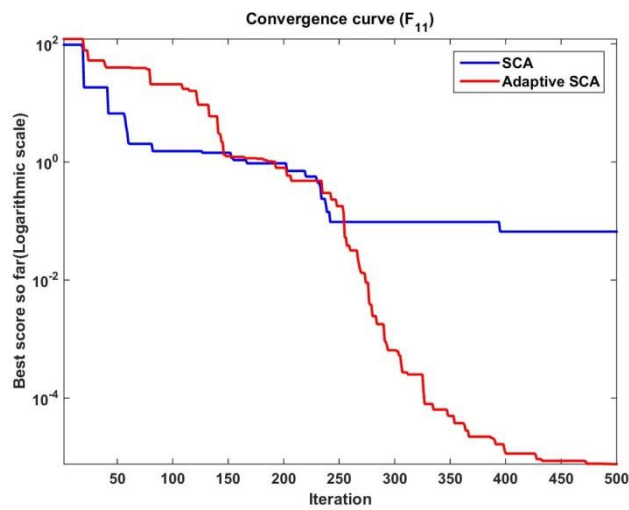
$F_9$



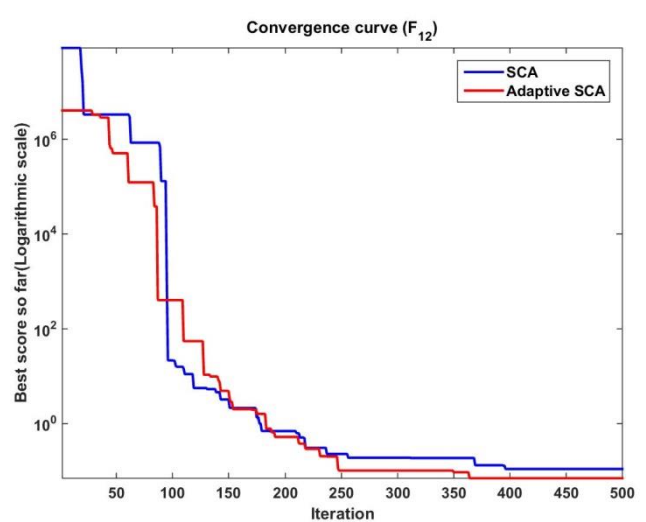
$F_{10}$



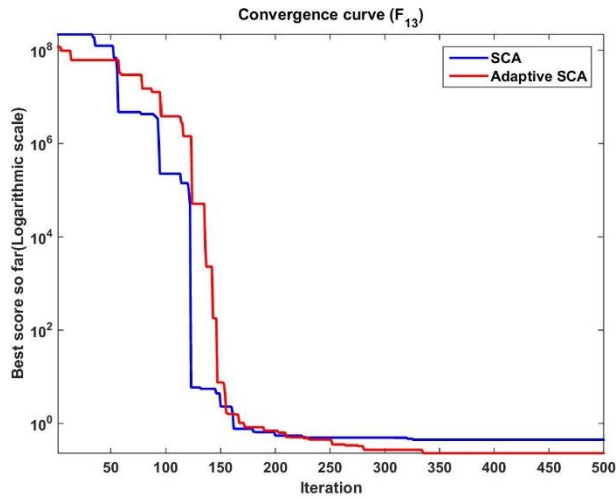
$F_{11}$



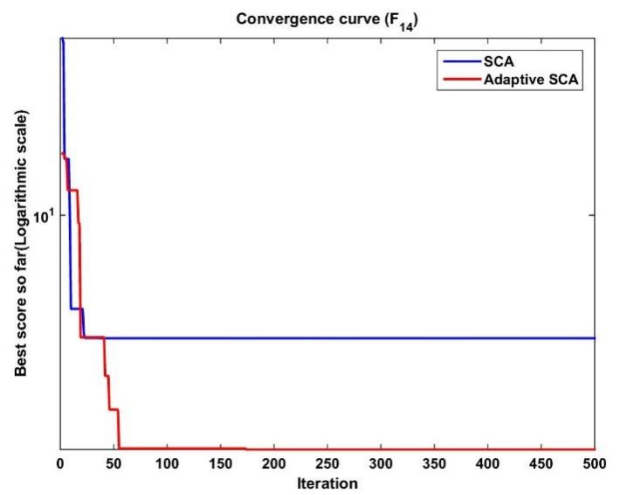
$F_{12}$



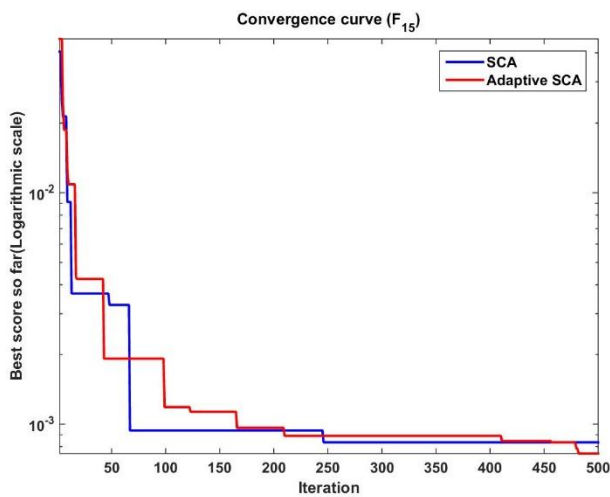
$F_{13}$



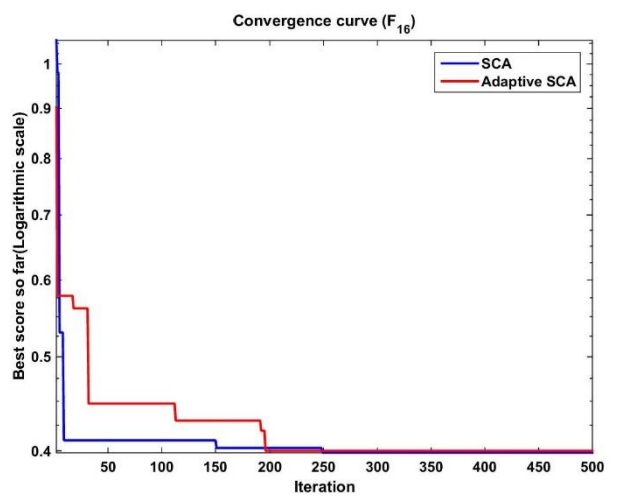
$F_{14}$



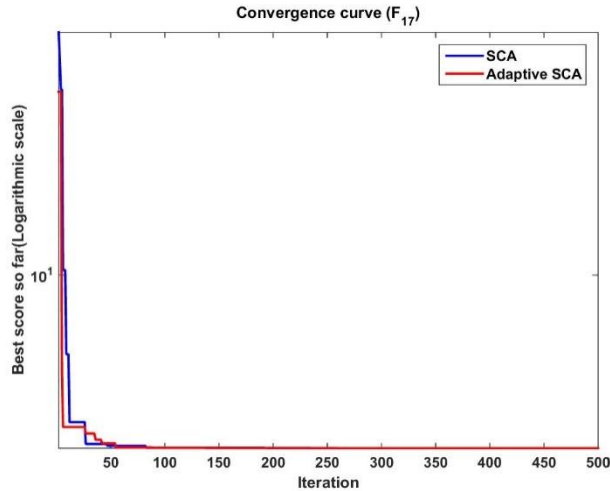
$F_{15}$



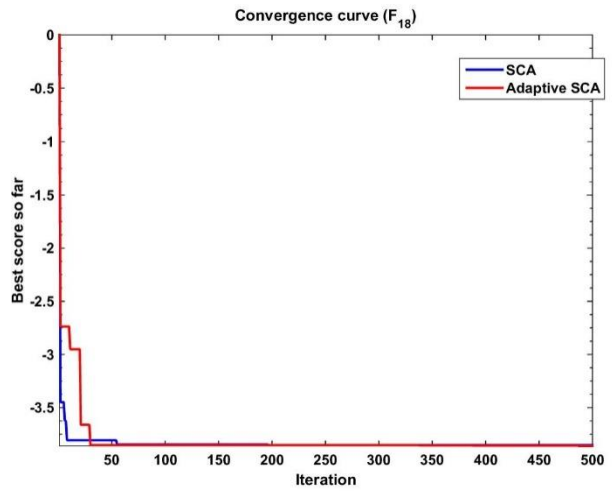
$F_{16}$



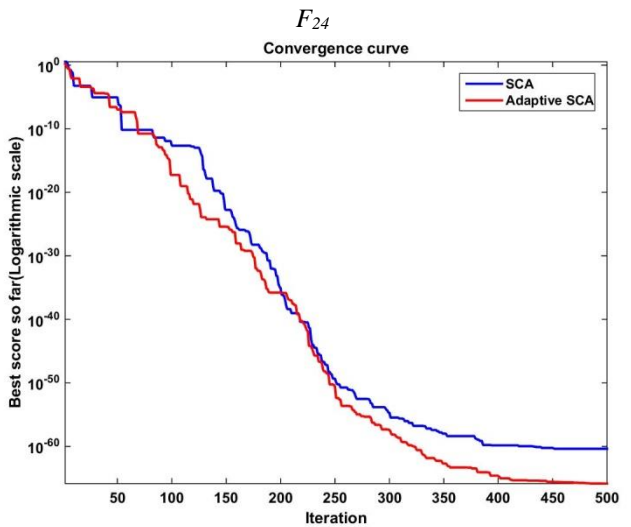
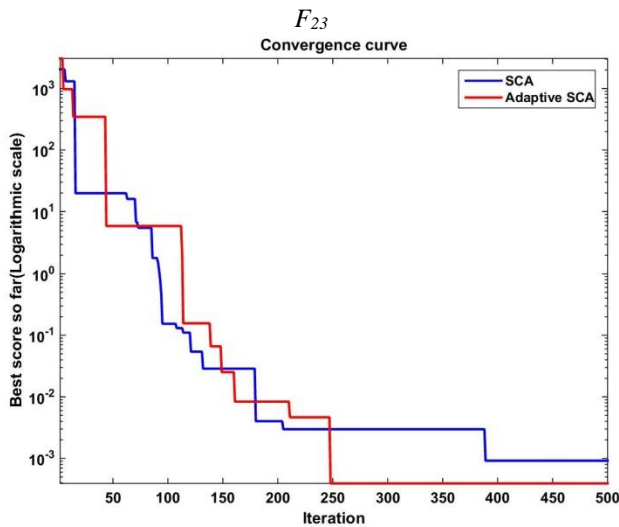
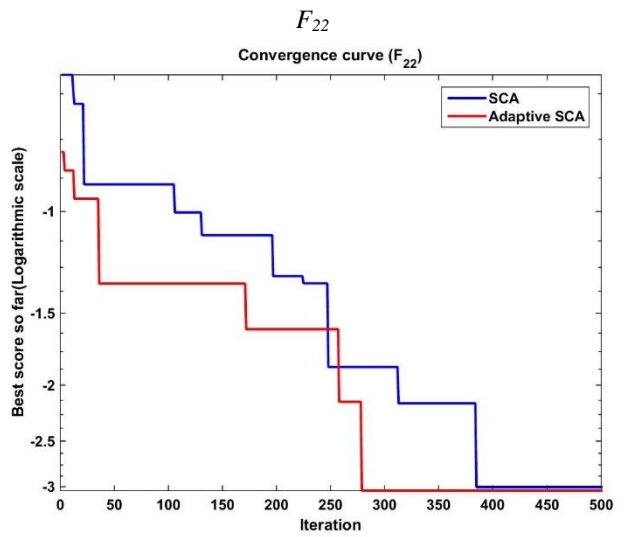
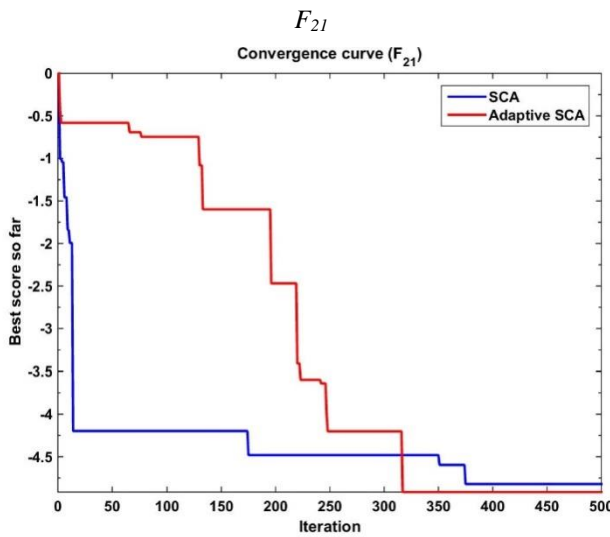
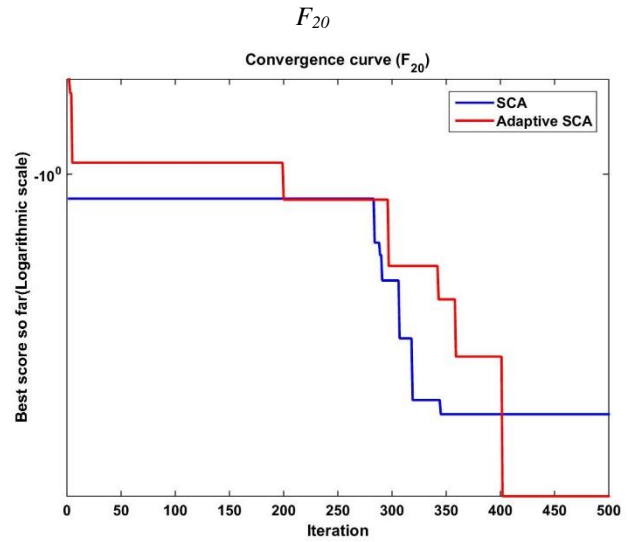
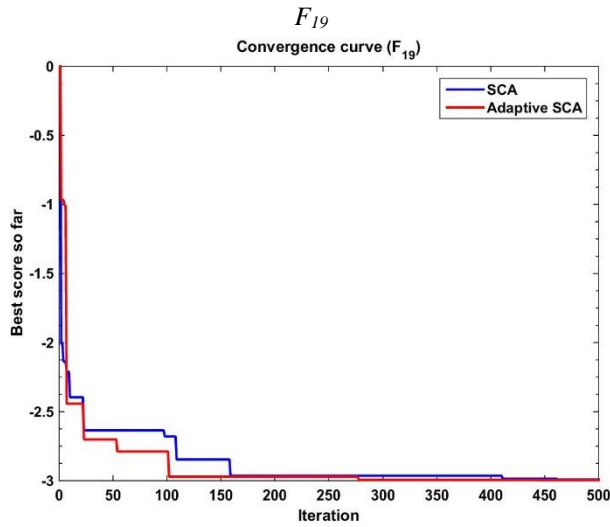
$F_{17}$



$F_{18}$







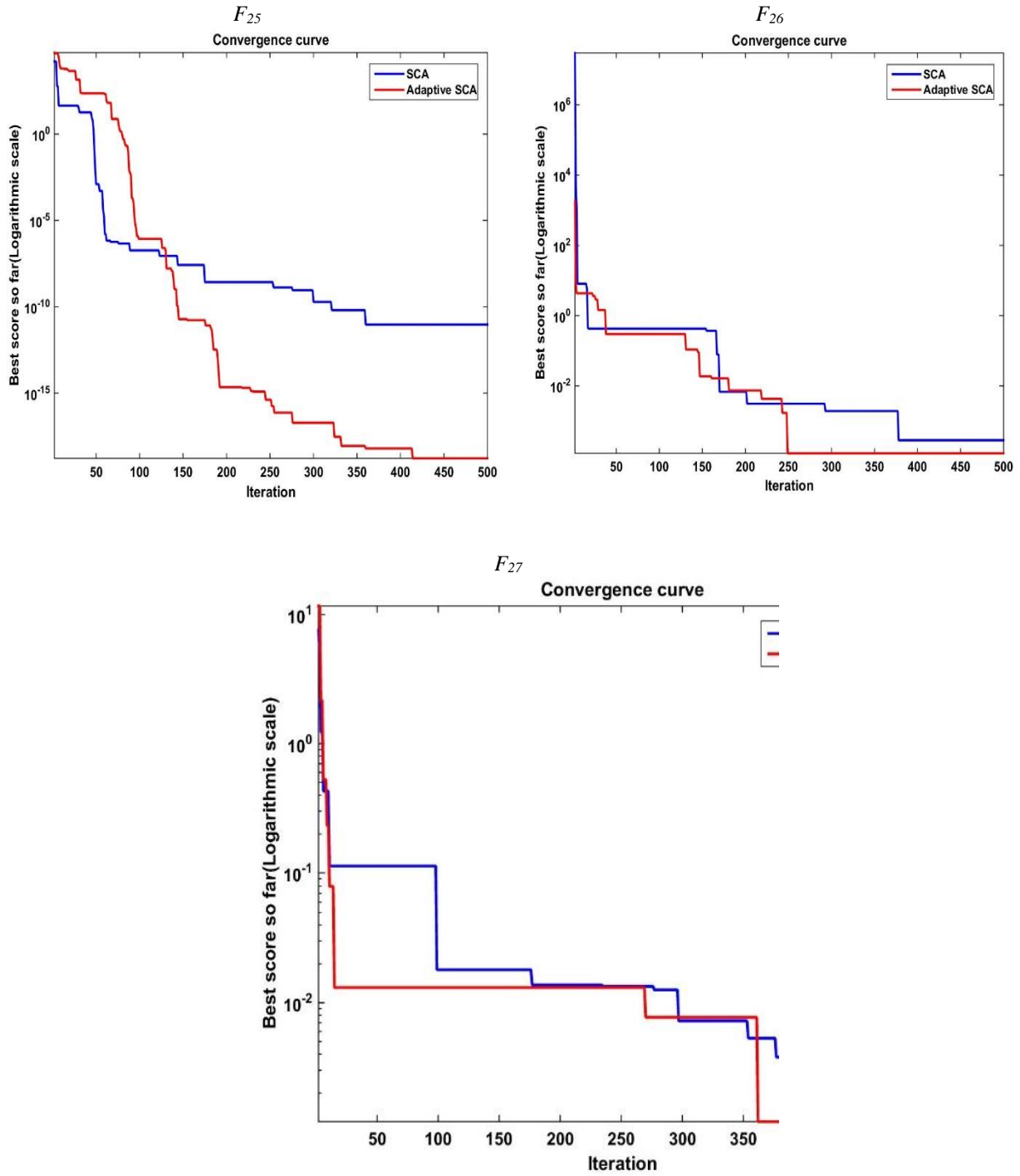


Fig. 3: Convergence Curve of Benchmark Test Function

Function	Sine Cosine Algorithm ( SCA )			Adaptive Sine Cosine ( ASCA )		
	Ave	Best	S.D.	Ave	Best	S.D.
F1	3.8997e-12	8.3555e-15	5.5031e-12	1.7034e-12	<b>4.0258e-15</b>	2.4033e-12
F2	5.1665e-10	5.1897e-11	6.5725e-10	5.3969e-09	<b>3.9446e-13</b>	7.6318e-09
F3	0.00013506	3.3344e-05	0.00014385	0.0058211	<b>8.9735e-10</b>	0.0082323
F4	0.000742	0.00071183	4.406e-05	0.0005013	<b>8.1901e-05</b>	0.00059317
F5	7.7006	7.6561	0.063	7.229	<b>7.0821</b>	0.20769
F6	0.4714	0.46241	0.012717	0.42624	<b>0.39943</b>	0.037903
F7	0.003145	0.0017773	0.001934	0.0012295	<b>0.0009001</b>	0.00046579
F8	-1985.6903	-2069.077	117.9266	-1972.6406	<b>-2083.7554</b>	157.1401
F9	1.6053e-05	6.6446e-07	2.1763e-05	0.02279	<b>4.2483e-10</b>	0.032231
F10	3.7458e-07	1.7164e-07	2.8699e-07	2.8647e-07	<b>3.702e-09</b>	3.9989e-07
F11	0.25018	0.065937	0.26056	0.16032	<b>7.6143e-06</b>	0.22672
F12	0.12648	0.11063	0.022422	0.070762	<b>0.070649</b>	0.00015947
F13	0.46522	0.4481	0.024212	0.26267	<b>0.23023</b>	0.045889
F14	2.9821	2.9821	9.2755e-09	1.0066	<b>1</b>	0.0093312
F15	0.001196	0.00083446	0.000511	0.0011316	<b>0.0007462</b>	0.00054495
F16	0.40079	0.39819	0.003682	0.40015	<b>0.4001</b>	7.8362e-05
F17	3.0002	<b>3</b>	0.000287	3.0001	<b>3</b>	8.5167e-05
F18	-3.851	-3.8518	0.001083	-3.8568	<b>-3.8597</b>	0.0040662
F19	-2.7927	-2.9917	0.2814	-2.9949	<b>-2.9951</b>	0.0003133
F20	-3.6866	-4.712	1.4501	-7.3322	<b>-8.001</b>	0.94579
F21	-4.033	-4.8214	1.1149	-3.6175	<b>-4.9149</b>	1.8349
F22	-2.9039	-3.0035	0.14096	-1.9953	<b>-3.0464</b>	1.4866
F23	0.0025187	0.00091794	0.0022638	0.00051534	<b>0.0003917</b>	0.00017479

F24	4.0003e-59	4.238e-61	5.5973e-59	1.4976e-61	<b>1.4385e-66</b>	2.1179e-61
F25	5.3868e-08	9.2165e-12	7.6168e-08	2.2212e-10	<b>1.6589e-19</b>	3.1412e-10
F26	0.00034411	0.00028346	8.577e-05	0.00034544	<b>0.0001207</b>	0.00031783
F27	0.0027642	0.0021221	0.00090814	0.0012886	<b>0.0012011</b>	0.00012384

Table 3: Result for Benchmark Functions

**V. ACOUSTIC PD LOCALIZATION SENSOR POSITION**

Dielectric breakdown in transformers is most frequently initiated by partial discharges. The consequences of these types of occurrences can be hazardous if not detected in a timely fashion. Regular PD analysis gives an accurate indication of the status of the deterioration process. So it is possible to foretell developing fault condition by online monitoring and precautionary tests. It is very much essential to have information of PD level and location to plan maintenance of electrical equipment. A famous method of understanding the health of the transformer is by studying the partial discharge signals. Monitoring of transformer can be either online or offline. The primary established techniques for electrical PD detection by measuring current or Radio Frequency (RF) pulses. Suppression of interference is one of the main challenges in detecting PDs, either while the transformer is off-line or on-line in a noisy environment. The off-line PD detection methods only provide snapshots in time of part of the transformer’s condition. On the other hand, no standards have yet been developed for on-line electrical monitoring of PDs.

It is well known that the occurrence of discharge results in discharge current or voltage pulse, electromagnetic impulse radiation, ultrasonic impulse radiation and visible or ultraviolet light emission. Accordingly, there are several detection methods that have been developed to measure those phenomena respectively. Acoustic detection is one of them which is very famous nowadays. PD generates acoustic waves in range of 20 kHz to 1 MHz. External system and internal system are two categories of acoustic detection techniques based on sensor location in transformer. External system is widely accepted as sensors are mounted outside of the transformer. An obvious advantage of the acoustic method is that it can locate the site of a PD by algorithms. Electromagnetic interference may cause corruption of signals captured by piezoelectric sensors.

A main objective is to determine the position of the PD source based on signals captured by sensor array inside the transformer tank as shown in Fig. 4. Each sensor will capture acoustic signals at different time as shown in Fig. 5. Time

Difference of Arrival (TDOA) algorithm has been implemented to find location of partial discharge source.

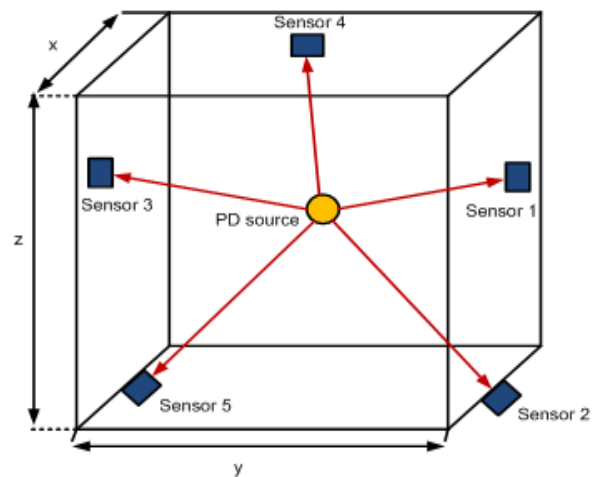


Fig. 4: Visualization of PD Source and Sensor Arrangement

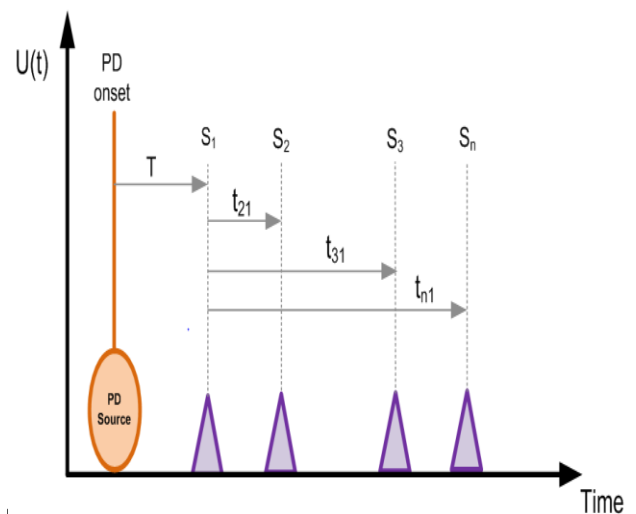


Fig. 5: Schematic of Acoustic Time Differences In Reference To Electrical PD signal

PDE equation in homogeneous medium for propagation of acoustic wave:

$$\frac{\partial^2 P}{\partial t^2} = v^2 \nabla^2 P = v^2 \left( \frac{\partial^2 P}{\partial x^2} + \frac{\partial^2 P}{\partial y^2} + \frac{\partial^2 P}{\partial z^2} \right) \dots (15)$$

Where:  $P(x, y, z, t)$  pressure wave field; function of space and time;  $x, y, z$  Cartesian co-ordinates (mm) and  $v$  acoustic wave velocity (m/s).

Element	X-axis (mm)	Y-axis (mm)	Z-axis (mm)
Transformer Dimension	5000	3000	4000
Actual PD source	4500	2600	3700
Sensor (S <sub>1</sub> )	2500	0	2000
Sensor (S <sub>2</sub> )	2500	1500	4000
Sensor (S <sub>3</sub> )	5000	1500	2000
Sensor (S <sub>4</sub> )	2500	3000	2000
Sensor (S <sub>5</sub> )	0	1500	2000
$t_1=2600$ micro-seconds (Reference)			

Table 4: Transformer Dimension and Co-Ordination Position of Sensor

$\tau_{i1}(\mu s) = [1600, 1500, 1900, 3524.69] - t_1, i = 2,3,4,5$ ,  
And sensor 1 is assumed as reference paper [6].

**• Problem Formulation:**

$$\tau_{21} = -1000 \times 10^{-03}, \tau_{31} = -1100 \times 10^{-03},$$

$$\tau_{41} = -700 \times 10^{-03}, \tau_{51} = -924.69 \times 10^{-03}, \quad (5)$$

$$P = \left[ (x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2 \right]^{0.5} \dots (6)$$

$$a = \left[ (x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2 \right]^{0.5} - P - v_e \tau_{21}; \quad (7)$$

$$b = \left[ (x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2 \right]^{0.5} - P - v_e \tau_{31}; \quad (8)$$

$$c = \left[ (x - x_4)^2 + (y - y_4)^2 + (z - z_4)^2 \right]^{0.5} - P - v_e \tau_{41}; \quad (9)$$

$$d = \left[ (x - x_5)^2 + (y - y_5)^2 + (z - z_5)^2 \right]^{0.5} - P - v_e \tau_{51}; \quad (10)$$

$$\text{Min } \{D_f(x, y, z, v_e)\} = a^2 + b^2 + c^2 + d^2; \quad (11)$$

Subjected to

$$\left. \begin{aligned} 0 \leq x \leq x_{\max} \\ 0 \leq y \leq y_{\max} \\ 0 \leq z \leq z_{\max} \\ 1200 \leq v_e \leq 1500, \quad (m/s) \end{aligned} \right\} \quad (12)$$

Where:

$x_{\max}, y_{\max}, z_{\max}$  and  $v_e$  are transformer tank dimension and equality sound velocity.

Calculated PD source is  $P_c(x_c, y_c, z_c)$  comprehensive distance error of it with actual PD source  $P(x, y, z)$  is

$$\Delta R = \left[ (x - x_c)^2 + (y - y_c)^2 + (z - z_c)^2 \right]^{0.5} \quad (13)$$

**• Error of each co-ordinate is formulated:**

$$\epsilon_r = \left| \frac{L_{act} - L_{cal}}{L_{act}} \right| \times 100\% \quad (14)$$

**• Maximum deviation  $D_{max}$**

$$D_{\max} = \max \left\{ \begin{matrix} |x_{act} - x_{cal}| \\ |y_{act} - y_{cal}| \\ |z_{act} - z_{cal}| \end{matrix} \right\} \dots\dots (15)$$

Where;  $L_{act}, x_{act}, y_{act}, z_{act}$  and  $L_{cal}, x_{cal}, y_{cal}, z_{cal}$  actual and calculated co-ordinates respectively.

Coordinate (mm)	Actual PD source	SCA	ASCA	GA [4]	PSO [4]	Linear PSO [4]	SA [4]	QGA [4]
x	4500	4357.3097	<b>4365.7179</b>	4223.76	4383.32	4382.14	4387.78	4394.77
y	2600	2394.7626	<b>2519.1891</b>	2391.71	2470.53	2469.99	2470.01	2475.98
z	3700	3634.2807	<b>3695.3759</b>	3503.04	3649.16	3648.11	3666.64	3656.17

Table 5: Comparison of the Results of PD localization

Error	SCA	ASCA	GA [4]	PSO [4]	Linear PSO [4]	SA [4]	QGA [4]
Error of x%	3.170	2.984	6.14	2.59	2.62	2.49	2.34
Error of y%	7.893	3.10	8.01	4.98	5.00	5.00	4.77
Error of z%	1.776	.0125	5.32	1.37	1.40	0.90	1.18
$D_{\max}$ /mm	205.2374	134.2831	276.24	129.47	130.01	129.99	124.02
Comprehensive Error( $\Delta R$ /mm)	258.4607	<b>156.7920</b>	398.10	181.55	182.99	174.94	168.45

Table 6: Error Analysis

**VI. CONCLUSION**

Sine Cosine Algorithm have an ability to find out optimum solution with constrained handling which includes both equality and inequality constraints. While obtaining optimum solution constraint limits should not be violated. Randomization plays an important role in both exploration and exploitation. Adaptive technique causes faster convergence, randomness, and stochastic behavior for improving solutions. Adaptive technique also used for random walk in search space when no neighboring solution exists to converse towards optimal solution. Acoustic PD source localization method based on ASCA is feasible. PD localization by ASCA gives better result than SCA and also accurate in compare to GA, PSO and linear PSO, SA and QGA algorithm. The ASCA result of various unconstrained problems proves that it is also an effective method in solving challenging problems with unknown search space.

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